

Elliptic flow of baryon-rich matter

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- ❑ Beam energy scan at RHIC
- ❑ Particle and antiparticle elliptic flows
- ❑ Hadronic potentials in nuclear medium
- ❑ Effects of hadronic potentials on elliptic flow
- ❑ Partonic potentials in QGP
- ❑ Effects of partonic potentials on elliptic flow
- ❑ QCD phase diagram

Based on work with Jun Xu, Lie-Wen Chen & Zi-wei Lin [PRC 85, 041901(R) (2012)]; Taesoo Song, Vincenzo Greco, Salvatore Plumari & Feng Li [arXiv:1211.5511 [nucl-th]]; Xu, Song & Li, [arXiv:1308.1753 [nucl-th]]

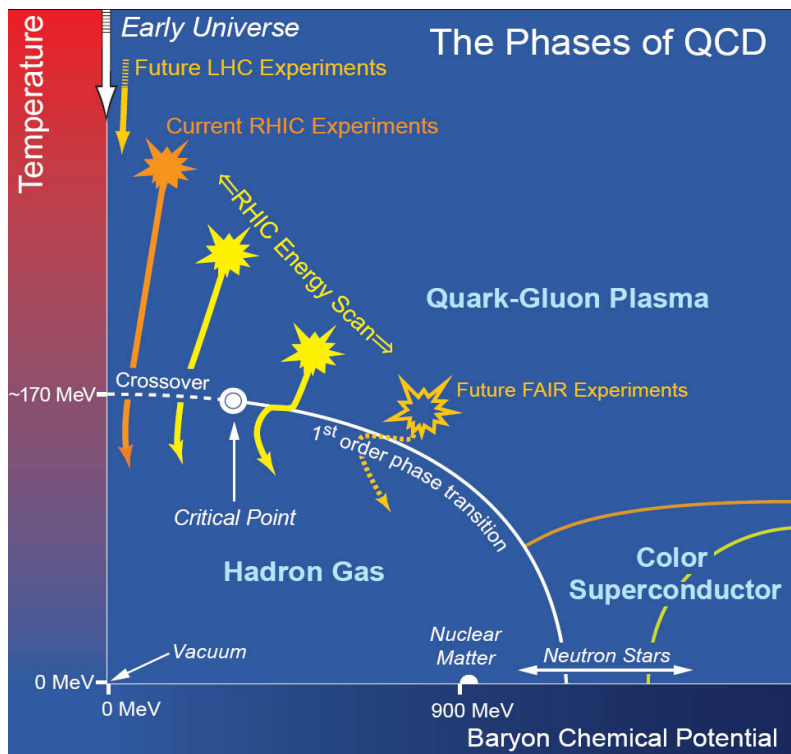
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Beam energy scan at RHIC

STAR Collaboration, arXiv: 1007.2613;
1106.5902 [nucl-ex]

Motivations:

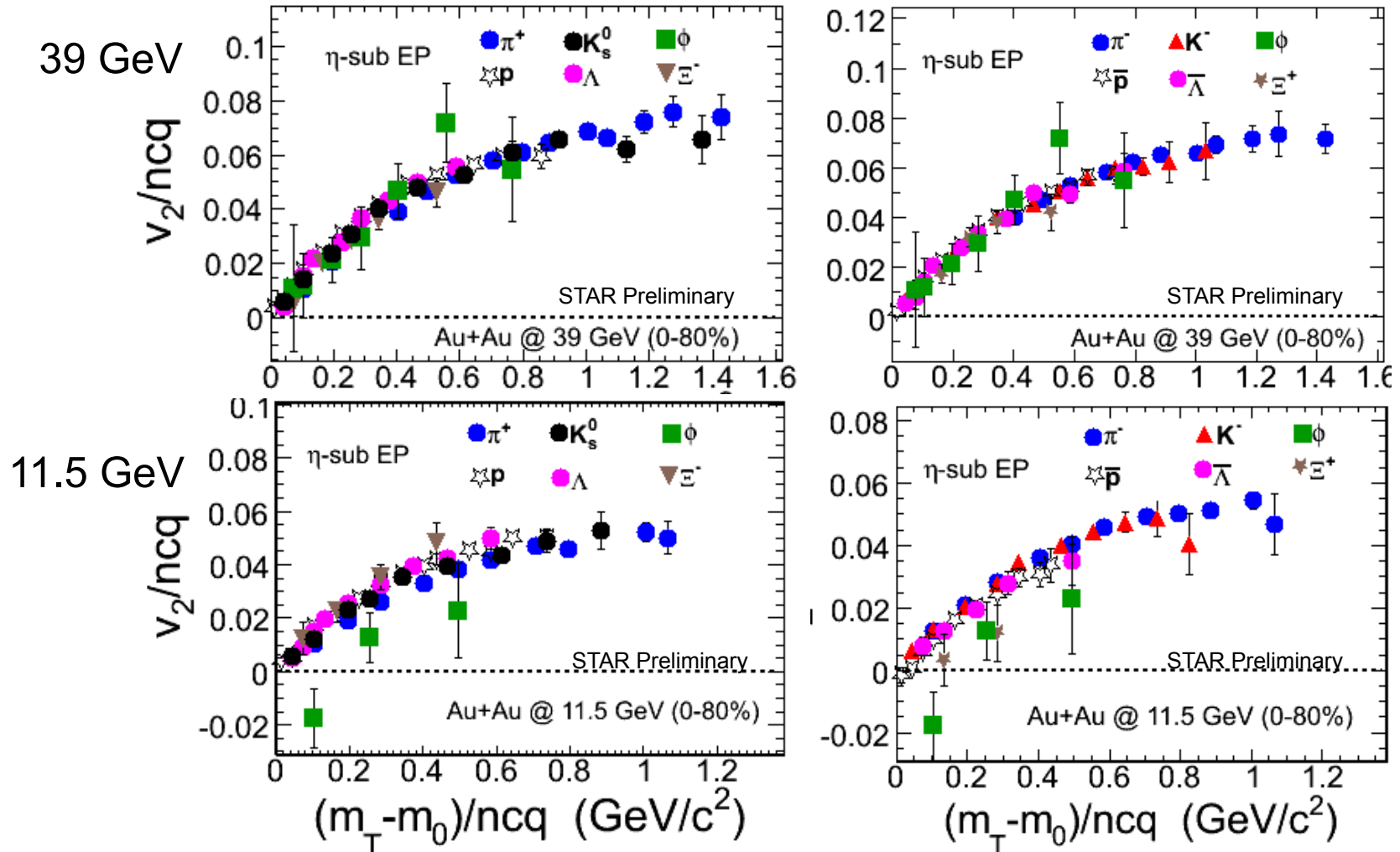
To study QCD phase diagram at finite baryon chemical potential: critical point (CP), onset of de-confinement



Experimental observations:

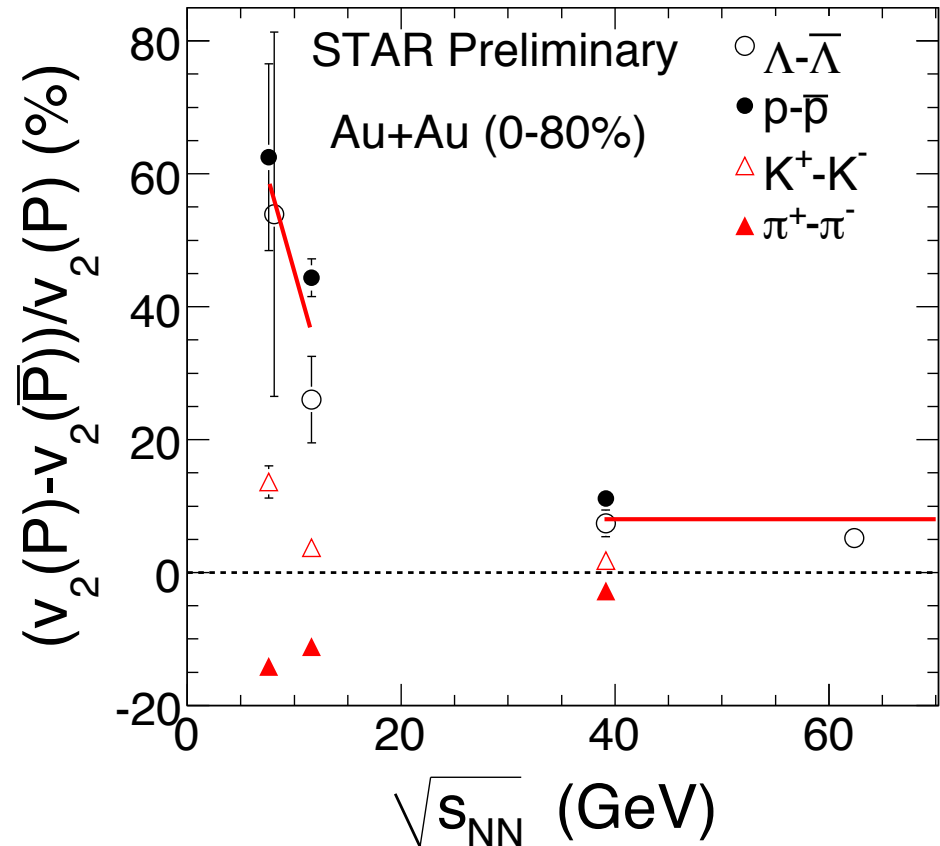
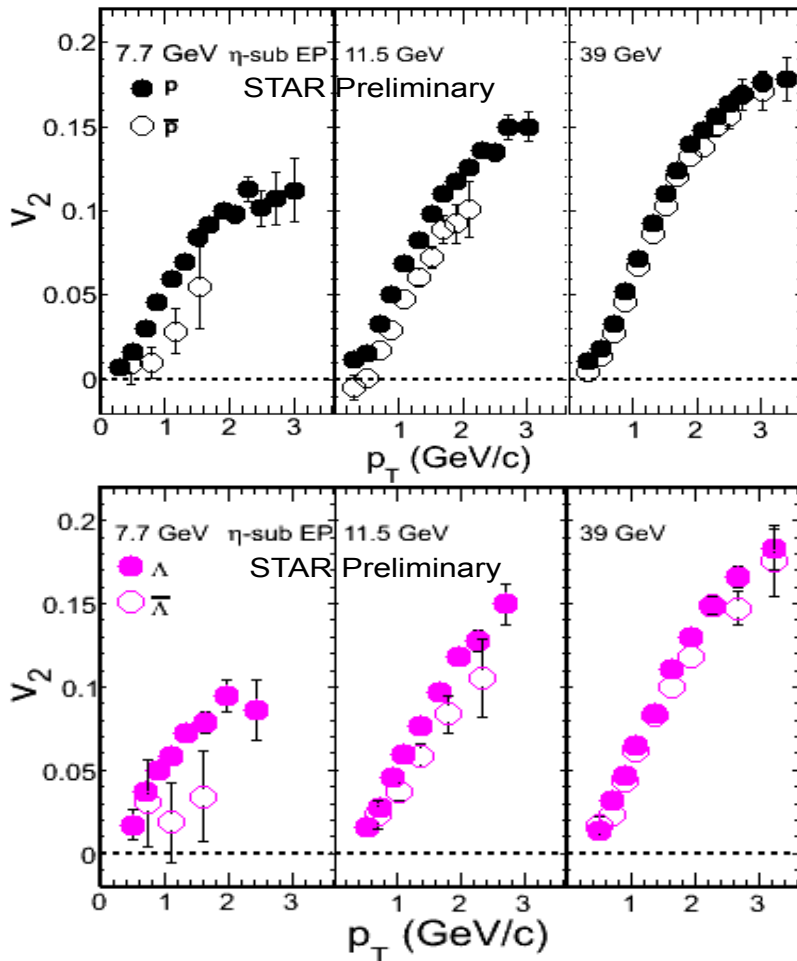
- **Particle ratios:** increasing baryon chemical potential with decreasing beam energy (DBE), reaching ~ 400 MeV at $s_{NN}^{1/2} = 7.7$ GeV
- **Dynamic charge correlations:** decreasing difference in same and opposite charges correlations with DBE (hadronic dominance?)
- **Freeze-out eccentricity:** increasing with DBE (softening of EOS?)
- **Directed flow:** dv_1/dy changes sign (softening of EOS?) and increasing difference in proton and antiproton dv_1/dy with DBE (hadronic dominance?)
- **Moments of net-proton distributions:** both skewness and kurtosis deviate from HRG for $s_{NN}^{1/2} < 39$ GeV (presence of CP?)
- **Particle ratio fluctuations:** nonzero $v_{dyn}(K/\pi)$ (correlated emission or presence of CP?)
- **Elliptic flow:** breakdown of NCQ scaling and increasing difference between particles and anti-particles with DBE (hadronic dominance? chiral magnetic effect?)

Beam energy dependence of CQN scaled elliptic flow



- Phi meson falls off trend at $s^{1/2}_{NN} = 11.5$ GeV (hadronic dominance?)

Particle and antiparticle elliptic flows



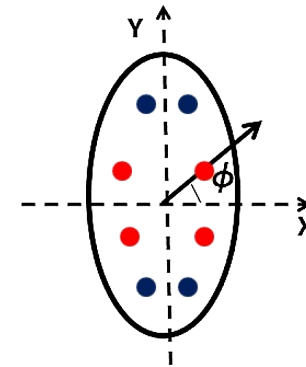
- Particle and antiparticle elliptic flows become significantly different below $s_{NN}^{1/2} < 11.5$ GeV: $v_2(\text{baryon}) > v_2(\text{anti-baryon})$, $v_2(K^+) > v_2(K^-)$, and $v_2(\pi^+) < v_2(\pi^-)$
- P_T -integrated relative v_2 difference between particles and antiparticles: **63%**, **44%**, and **12%** for (p, pbar), **53%**, **25%**, and **7%** for (Λ , $\bar{\Lambda}$), **13%**, **3%**, and **1%** for (K^+ , K^-), **-15%**, **-10%**, and **-3%** for (π^+ , π^-) at **7.7**, **11.5**, and **39** GeV

Possible explanations for different particle and antiparticle elliptic flows

- **Chiral magnetic wave** [Bumier, Kharzeev, Liao & Yee, PRL 107, 052303 (2011)]

- Stemming from the coupling of the density waves of electric and chiral charge induced by the axial anomaly in the presence of an external magnetic field

$$j_V = \frac{N_c e}{2\pi^2} \mu_A B, \quad j_A = \frac{N_c e}{2\pi^2} \mu_V B$$



- Electric quadrupole moment in QGP
- radial flow leads to decreasing positive hadron and increasing negative hadron elliptic flows
- $v_2(\pi^+) < v_2(\pi^-)$

- Effects on p and \bar{p} as well as K^+ and K^- are masked by different absorption cross sections

- **Transport versus produced particles** [Dunlop, Lisa & Sorensen, PRC 84, 044914 (2011)]: Larger elliptic flow for transport than for produced (anti)particles

- **Different particle and antiparticle transport coefficients** [Greco, Mitrovski & Torrieri, PRC 86, 044905 (2012)] : Large absorption cross sections for antiparticles

- **Baryon charge, strangeness and isospin conservations** [Steinheimer, Koch & Bleicher, PRC 86, 044903 (2012)]: Decreasing p_{bar}/p ratio with radial distance

- **Different particle and antiparticle potentials** [Xu, Chen, Lin & Ko, PRC 85, 041901(R) (2012)]: Repulsive potential for particles and attractive potential for antiparticles

- **Different quark and antiquark potentials** [Song, Plumari, Greco, Ko & Li, arXiv:1211.5511 [nucl-th]]: Repulsive vector potential for quarks and attractive one for antiquarks

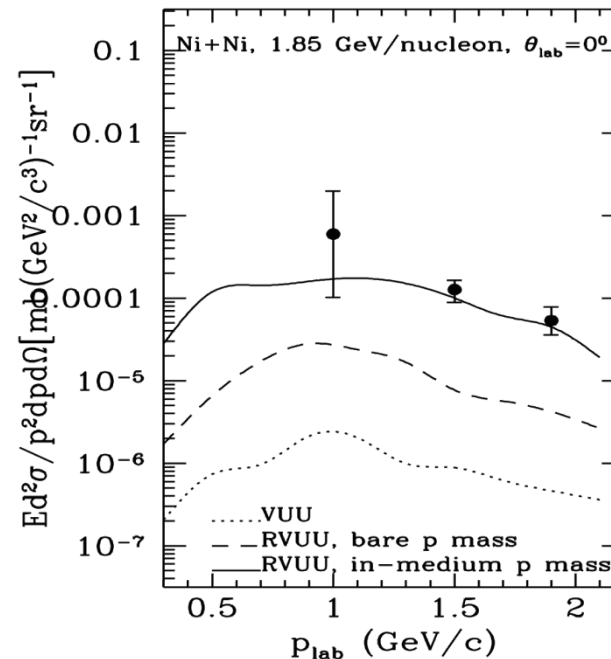
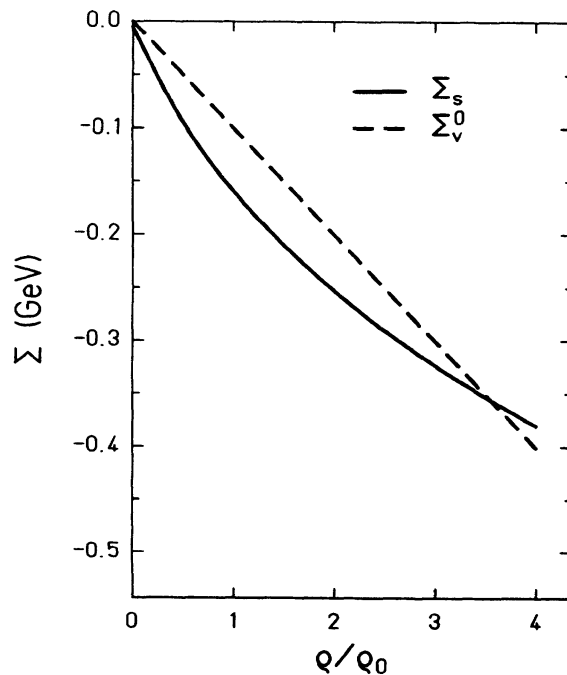
Hadronic potentials in nuclear medium (I)

Ko & Li, JPG 22, 1673 (1996); Ko, Koch & Li, ARNPS 47, 505 (1997)

- **Nucleons and antinucleons:** Relativistic mean-field model → attractive scalar potential Σ_s and repulsive vector potential Σ_v (“+” for nucleons and “-” for antinucleons due to G-parity)

$$U_{N,\bar{N}}(\rho_s, \rho_B) = \Sigma_s(\rho_s, \rho_B) \pm \Sigma_v^0(\rho_s, \rho_B) = \frac{g_\sigma^2}{m_\sigma^2} \rho_s \pm \frac{g_\omega^2}{m_\omega^2} \rho_B$$

$$U_N = -60 \text{ MeV}, U_{\bar{N}} = -260 \text{ MeV at } \rho_0 = 0.16 \text{ fm}^{-3}$$



- Deep antiproton attractive potential reduces its production threshold and thus enhances its yield in subthreshold heavy ion collisions

Hadronic potentials in nuclear medium (II)

Ko & Li, JPG 22, 1673 (1996); Ko, Koch & Li, ARNPS 47, 505 (1997)

- **Kaons and antikaons:** Chiral effective Lagrangian \rightarrow repulsive potential for kaons and attractive potential for antikaons

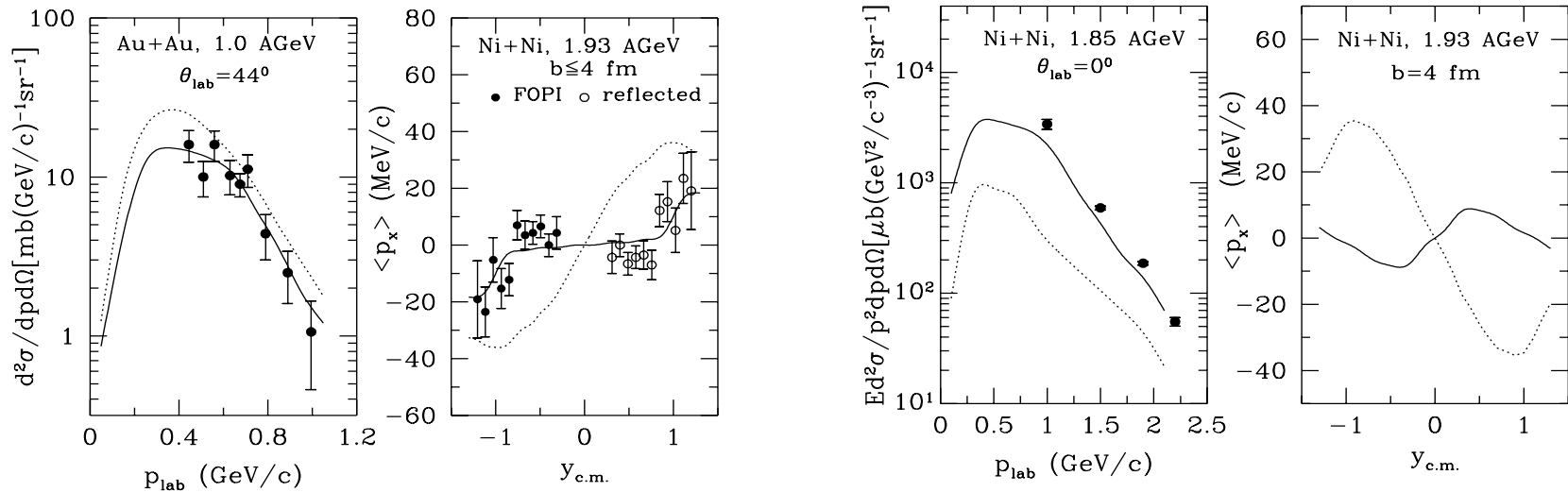
$$U_{K\bar{K}} = \omega_{K\bar{K}} - \omega_0, \quad \omega_0 = \sqrt{m_K^2 + p^2}$$

$$\omega_{K\bar{K}} = \sqrt{m_K^2 + p^2 - a_{K\bar{K}}\rho_s + (b_K\rho_B)^2} \pm b_K\rho_B$$

$$a_K = 0.22 \text{ GeV}^2 \text{ fm}^3, \quad a_{\bar{K}} = 0.45 \text{ GeV}^2 \text{ fm}^3$$

$$b_K = 0.33 \text{ GeV}^2 \text{ fm}^3$$

$$\Rightarrow U_K = 20 \text{ MeV}, U_{\bar{K}} = -120 \text{ MeV at } \rho_0 = 0.16 \text{ fm}^{-3}$$

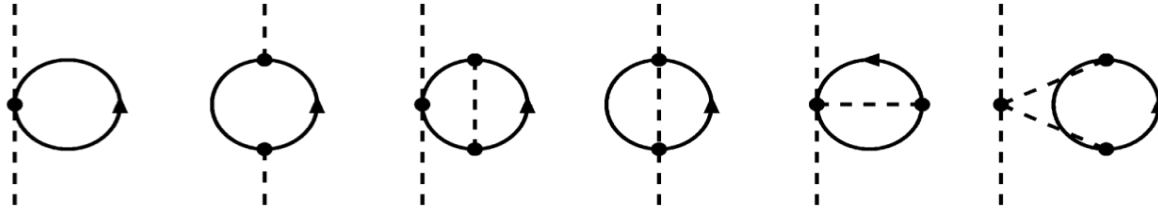


- Experimental data on spectrum and directed flow are consistent with repulsive kaon and attractive antikaon potentials

Hadronic potentials in nuclear medium (III)

Kaiser & Weise,
PLB 512, 283 (2001)

- **Pions:** $U_\pi = \Pi/(2m_\pi)$ in terms of pion selfenergies



$$\Pi^-(\rho_n, \rho_p) = \rho_n [T_{\pi N}^- - T_{\pi N}^+] - \rho_p [T_{\pi N}^- + T_{\pi N}^+] + \Pi_{\text{rel}}^-(\rho_n, \rho_p) + \Pi_{\text{cor}}^-(\rho_n, \rho_p)$$

$$\Pi^+(\rho_p, \rho_n) = \Pi^-(\rho_n, \rho_p)$$

$$\Pi^0(\rho_n, \rho_p) = -(\rho_p + \rho_n)T_{\pi N}^+ + \Pi_{\text{cor}}^0(\rho_n, \rho_p)$$

Isospin even and odd πN -scattering matrices extracted from energy shift and width of 1s level in pionic hydrogen atom

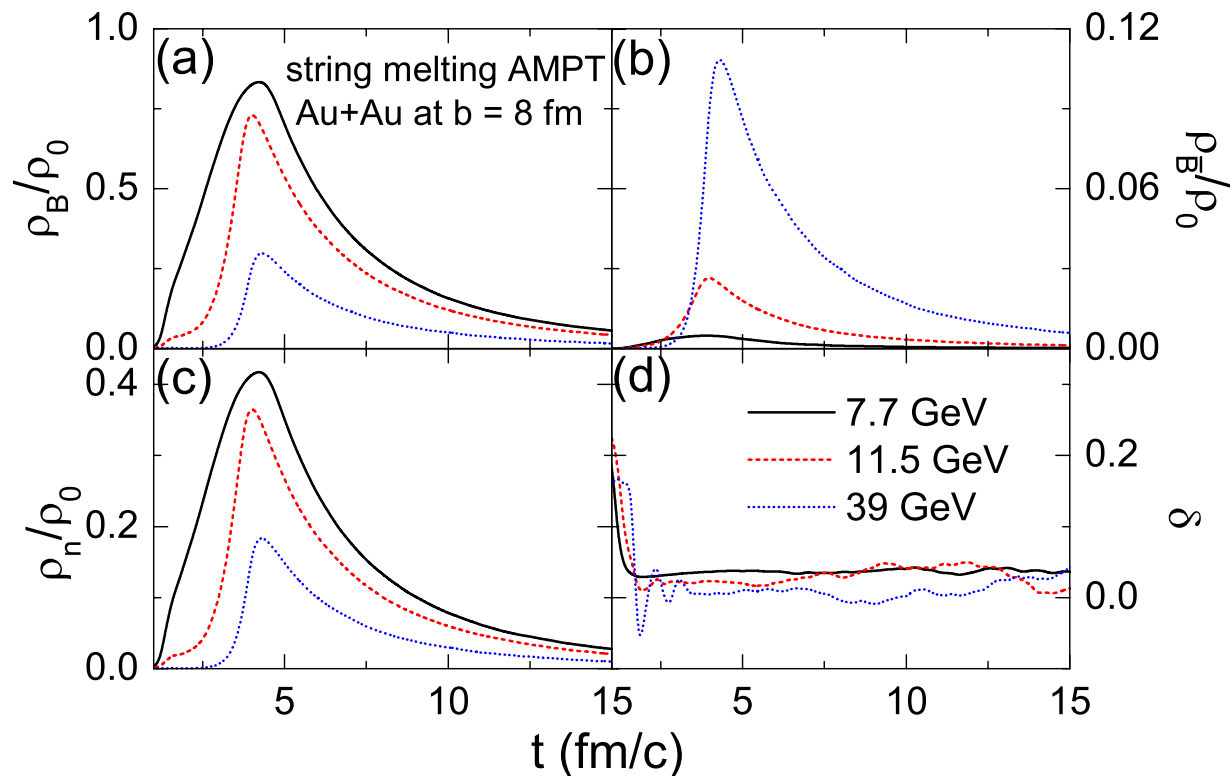
$$T_{\pi N}^+ \approx 1.847 \text{ fm} \quad \text{and} \quad T_{\pi N}^- \approx -0.045 \text{ fm}$$

At normal nuclear density $\rho=0.165 \text{ fm}^{-3}$ and isospin asymmetry $\delta=0.2$ such as in Pb,

$$U_{\pi^-} = 14 \text{ MeV}, \quad U_{\pi^+} = -1 \text{ MeV}, \quad U_{\pi^0} = 6 \text{ MeV}$$

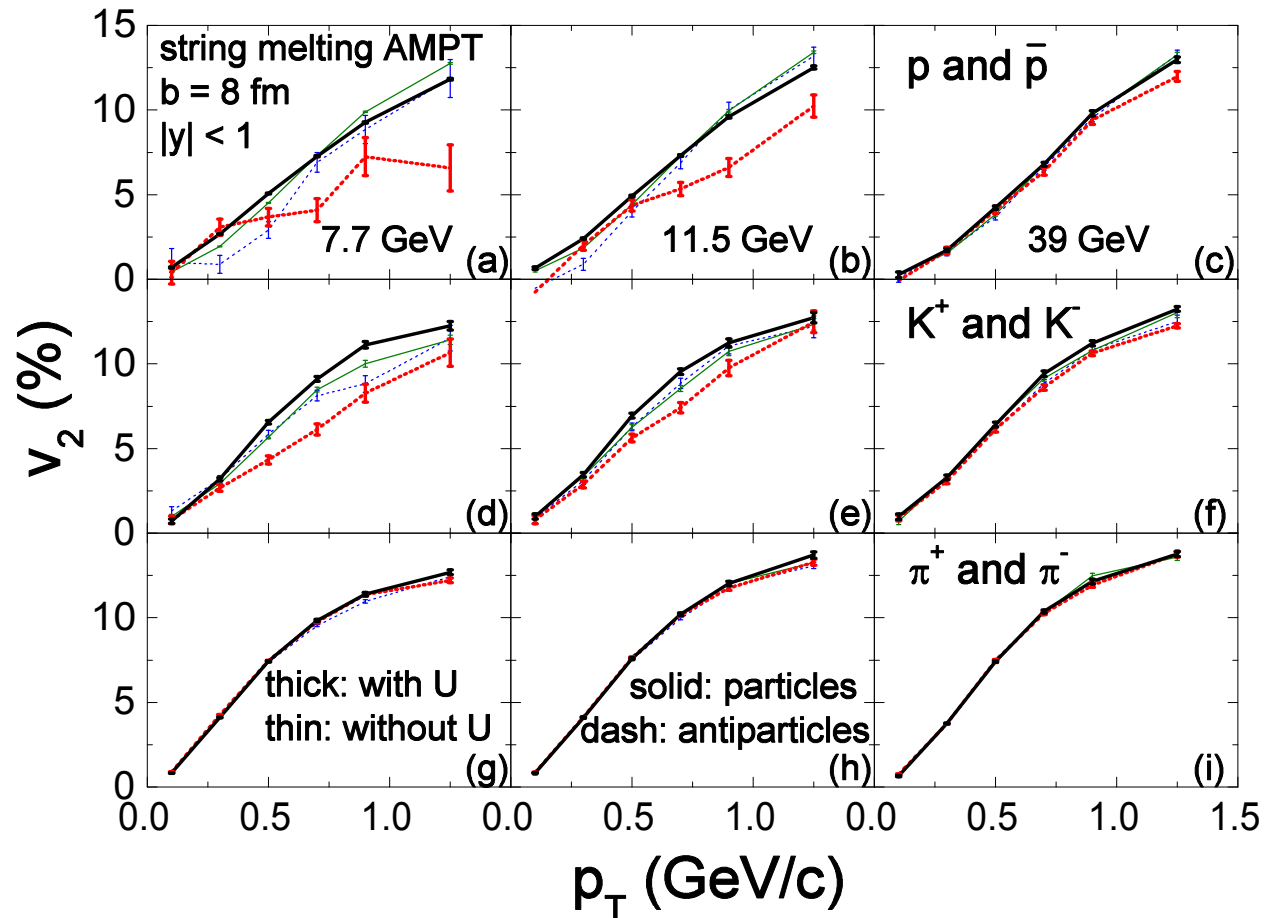
Hadron density evolutions in AMPT

Adjust parton scattering cross section and ending time of partonic stage to approximately reproduce measured elliptic flows and extracted hadronic energy density ($\sim 0.35 \text{ GeV}/\text{fm}^3$): isotropic cross sections of 3, 6 and 10 mb, and parton ending time of 3.5, 2.6, 2.9 fm/c for $s_{NN}^{1/2} = 7.7, 11.5, \text{ and } 39 \text{ GeV}$, respectively



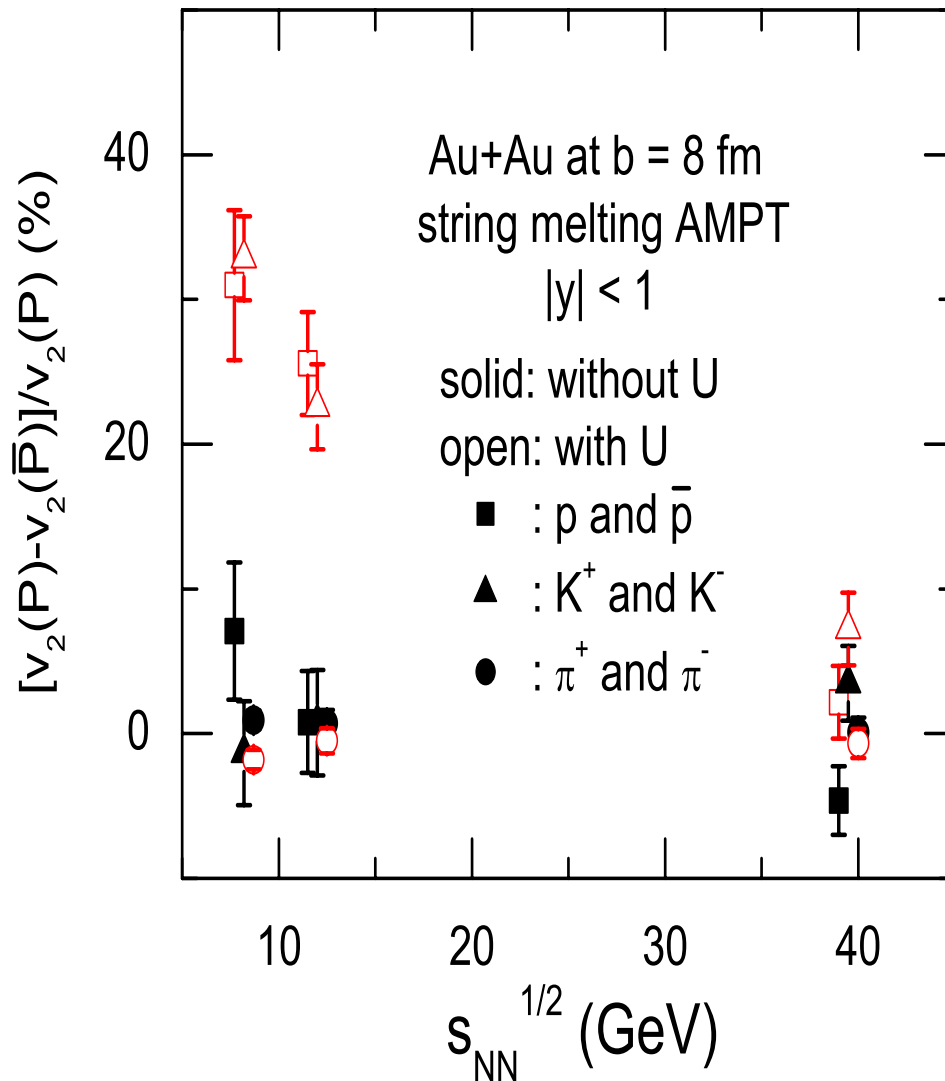
- Increasing baryon and decreasing antibaryon densities with decreasing energy
- Increasing neutron density with decreasing energy, but isospin asymmetry $\delta=0.02$ is small due to production of Λ hyperon and pions

Particle and antiparticle differential elliptic flows



- Similar particle and antiparticle elliptic flows without hadronic potentials
- Hadronic potentials increase slightly p and \bar{p} v_2 at $p_T < 0.5$ GeV but reduce slightly (strongly) p (\bar{p}) v_2 at high p_T
- Hadronic potentials increase slightly v_2 of K^+ and reduce v_2 of K^-
- Effects of hadronic potentials on π^+ and π^- v_2 are small

P_T-integrated particle and antiparticle elliptic flow difference



→ Hadronic potentials underestimate p-pbar and overestimate K^+ - K^- v_2 difference

- Difference very small without hadronic potentials → different particle and antiparticle scattering and absorption cross sections have small effects
- Hadronic potentials lead to relative v_2 difference between p and pbar and between K^+ and K^- of **30%** at 7.7 GeV, 20% at 11.5 GeV, and negligibly small value at 39 GeV, only very small negative value between π^+ and π^-
- Compared to experimental values of **63%**, 44%, and 12% for (p,pbar), **13%**, 3%, and 1% for (K^+ , K^-), **-15%**, -10%, and -3% for (π^+ , π^-) at 7.7, 11.5, and 39 GeV, ours are smaller for (p,pbar) and (π^+ , π^-) and larger for (K^+ , K^-)

Quark and antiquark potentials in QGP (I)

- NJL model [Bratovic, Hatsuda & Weise, PLB 719, 131 (2013)]

$$\begin{aligned}
 \mathcal{L} = & \bar{\psi}(i \not{\partial} - M)\psi + \frac{G}{2} \sum_{a=0}^8 \left[(\bar{\psi}\lambda^a\psi)^2 + (\bar{\psi}i\gamma_5\lambda^a\psi)^2 \right] && \text{Scalar-pseudoscalar} \\
 & + \sum_{a=0}^8 \left[\frac{G_V}{2} (\bar{\psi}\gamma_\mu\lambda^a\psi)^2 + \frac{G_A}{2} (\bar{\psi}\gamma_\mu\gamma_5\lambda^a\psi)^2 \right] && \text{Vector-axial vector} \\
 & - K \left[\det_f \left(\bar{\psi}(1 + \gamma_5)\psi \right) + \det_f \left(\bar{\psi}(1 - \gamma_5)\psi \right) \right], && \text{Kobayashi-Maskawa-} \\
 & && \text{t'Hooft (KMT)}
 \end{aligned}$$

where $\det_f(\bar{\psi}\Gamma\psi) = \sum_{i,j,k} \varepsilon_{ijk} (\bar{u}\Gamma q_i)(\bar{d}\Gamma q_j)(\bar{s}\Gamma q_k).$

- Mean-field approximation

$$\mathcal{L} = \bar{\psi} \left(i\partial^\mu - \frac{2}{3} G_V \langle \bar{\psi}\gamma^\mu\psi \rangle \right) \gamma_\mu \psi - \bar{\psi} M^* \psi + \dots$$

where $M^* = \text{diag}(M_u, M_d, M_s)$ with

$$\begin{aligned}
 M_u &= m_u - 2G \langle \bar{u}u \rangle + 2K \langle \bar{d}d \rangle \langle \bar{s}s \rangle & \langle \bar{q}_i q_i \rangle &= -2M_i N_c \int \frac{d^3\mathbf{k}}{(2\pi)^3 E_i} [1 - f_i(k) - \bar{f}_i(k)] \\
 M_d &= m_d - 2G \langle \bar{d}d \rangle + 2K \langle \bar{s}s \rangle \langle \bar{u}u \rangle & & \\
 M_s &= m_s - 2G \langle \bar{s}s \rangle + 2K \langle \bar{u}u \rangle \langle \bar{d}d \rangle & \langle \bar{\psi}\gamma^\mu\psi \rangle &= 2N_c \sum_{i=u,d,s} \int \frac{d^3\mathbf{k}}{(2\pi)^3 E_i} k^\mu [f_i(k) - \bar{f}_i(k)],
 \end{aligned}$$

Quark and antiquark potentials in QGP (II)

$$U_{q,\bar{q}} = \sqrt{M_q^2 + (\vec{p} \mp g_v \vec{\rho})^2} \pm g_v \rho_0 - \sqrt{m_q^2 + \vec{p}^2}$$

$$\text{Net baryon current: } \vec{\rho} = \langle \bar{\psi} \vec{\gamma} \psi \rangle \qquad g_v = \frac{2}{3} G_V$$

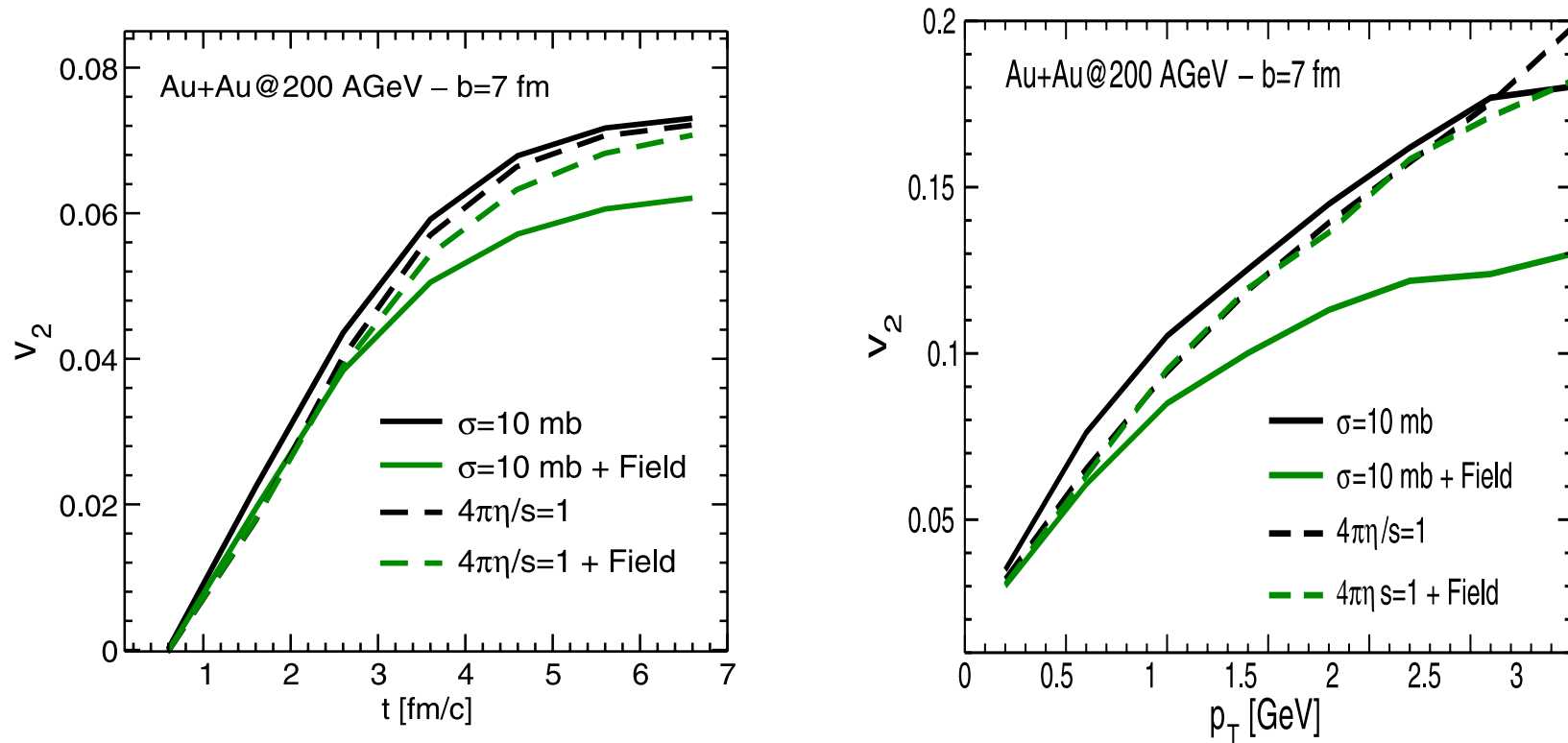
$$\text{Net baryon density: } \rho_0 = \langle \bar{\psi} \gamma^0 \psi \rangle$$

- Quark mass is modified by the quark condensate
 - attractive scalar potential on both quark and antiquark
- Vector potential is repulsive for quark and attractive for antiquark
 - enhances relative v_2 difference between quarks and antiquarks
 - enhances relative v_2 difference between p and pbar, Λ and Λ bar, K^+ and K^-

→ Would bring results with only hadronic potentials closer to experimental data

Effects of attractive scalar potential in quark matter

Plumari, Baran, Di Tori, Ferini, and Greco, PLB 689, 18 (2010)

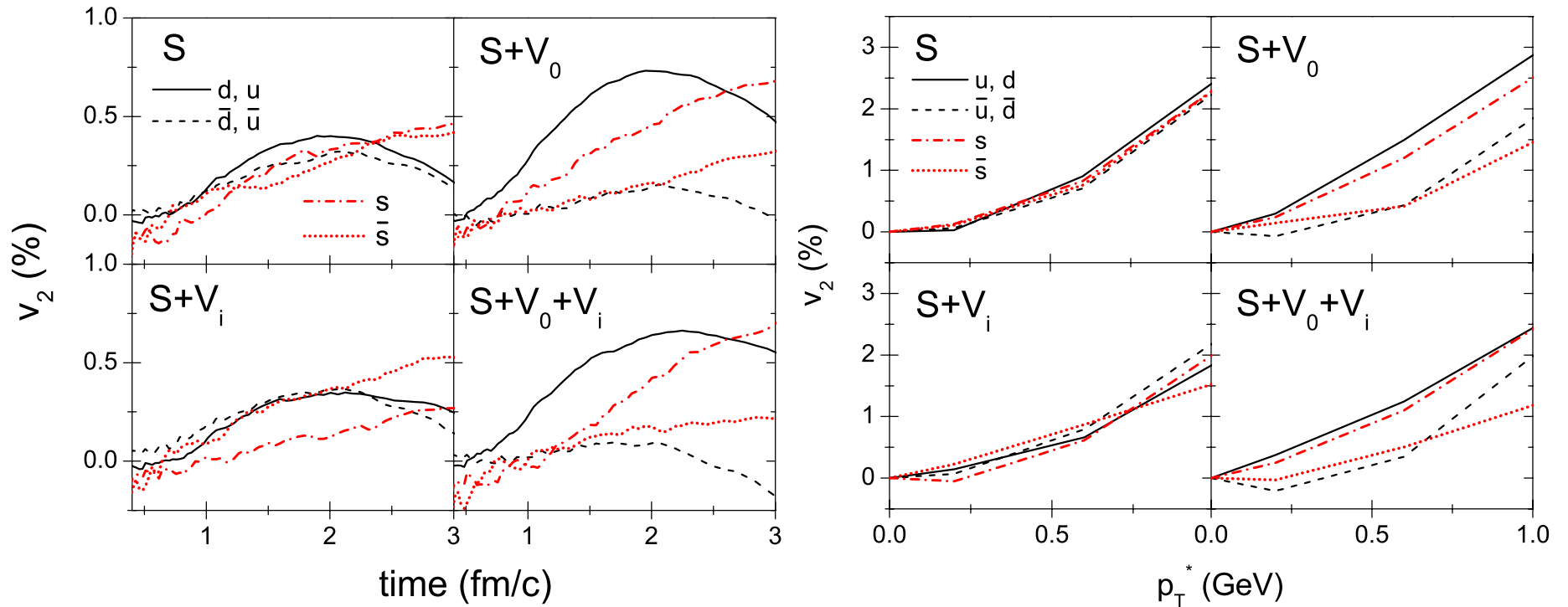


- Attractive scalar potential reduces v_2 of both quark and antiquark
- Effects are reduced when parton scattering cross section is large

Effects of vector potential in quark matter

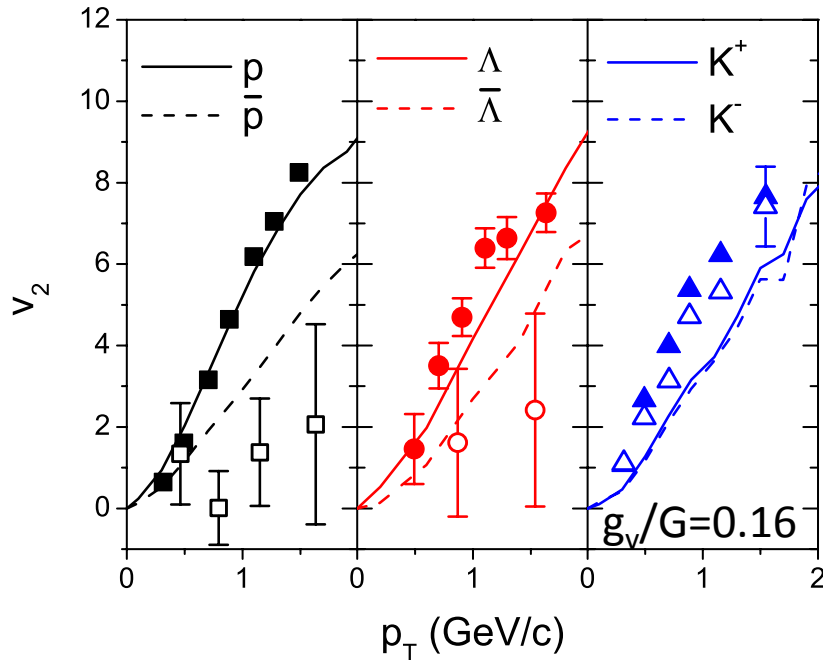
Using $m_u = m_d = 3.6$ MeV, $m_s = 87$ MeV, $G\Lambda^2 = 3.6$, $K\Lambda^5 = 8.9$, $\Lambda = 750$ MeV

Initial parton distributions from AMPT

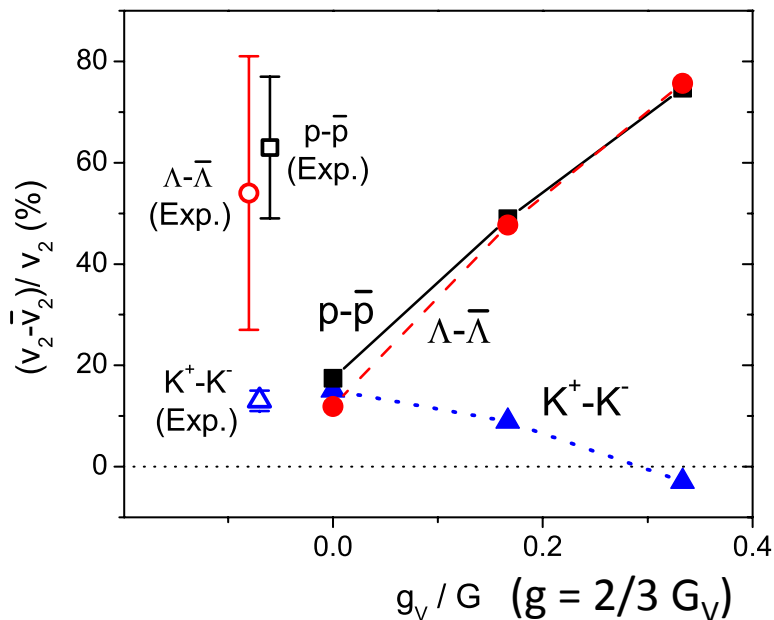


- Time (electric) component of vector potential increases quark but decreases antiquark elliptic flows
- Space (magnetic) component of vector potential has a similar effect at low p_T but an opposite effect at high p_T
- Net effect of vector potential: larger quark than antiquark elliptic flows

Partonic mean-field effects on hadron and antihadron v_2



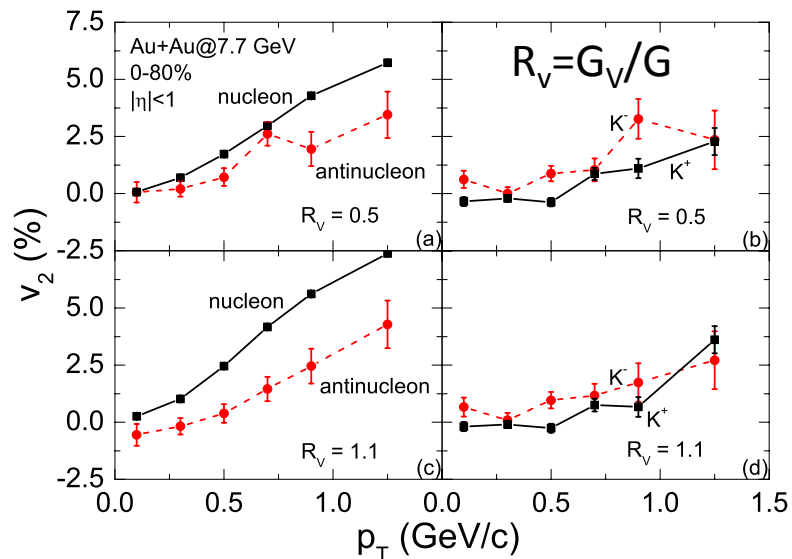
- Using recombination (coalescence) model to produce hadrons (proton, lambda, kaon) and their antiparticles from quarks and antiquarks at hadronization
- Smaller antiquark than quark v_2 leads to smaller v_2 for antiproton than proton, antilambda than lambda, and K^- than K^+



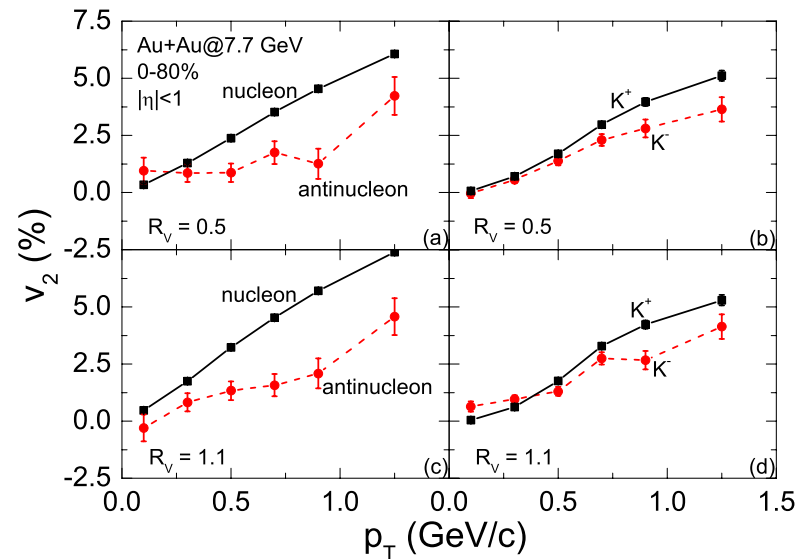
- Relative v_2 differences between proton and antiproton, lambda and antilambda, increase almost linearly with the strength of quark vector interaction
- Relative v_2 difference between K^+ and K^- decreases with the strength of quark vector interaction

Effects of hadronic evolution (mean fields + scattering)

Before hadronic evolution

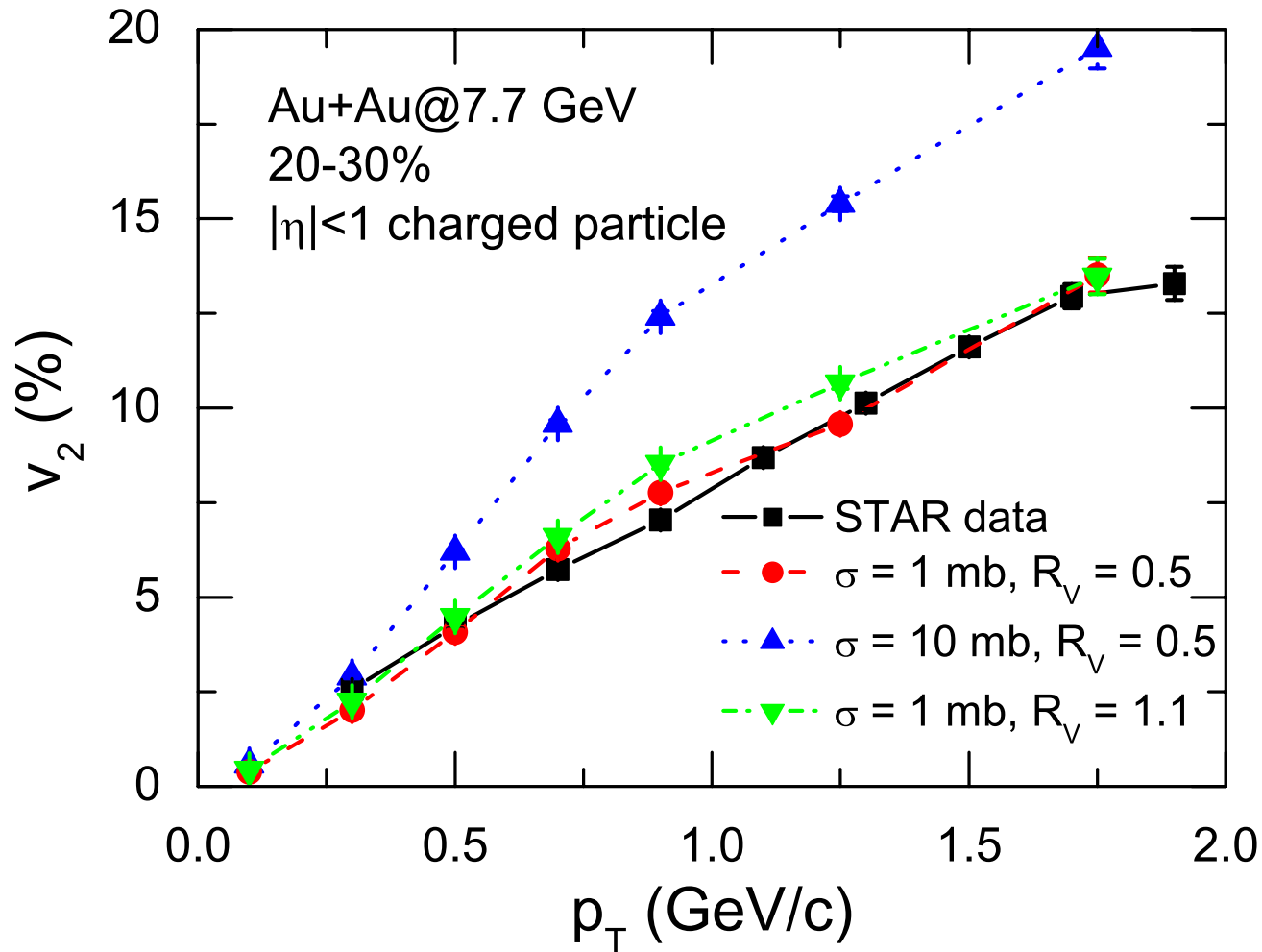


After hadronic evolution



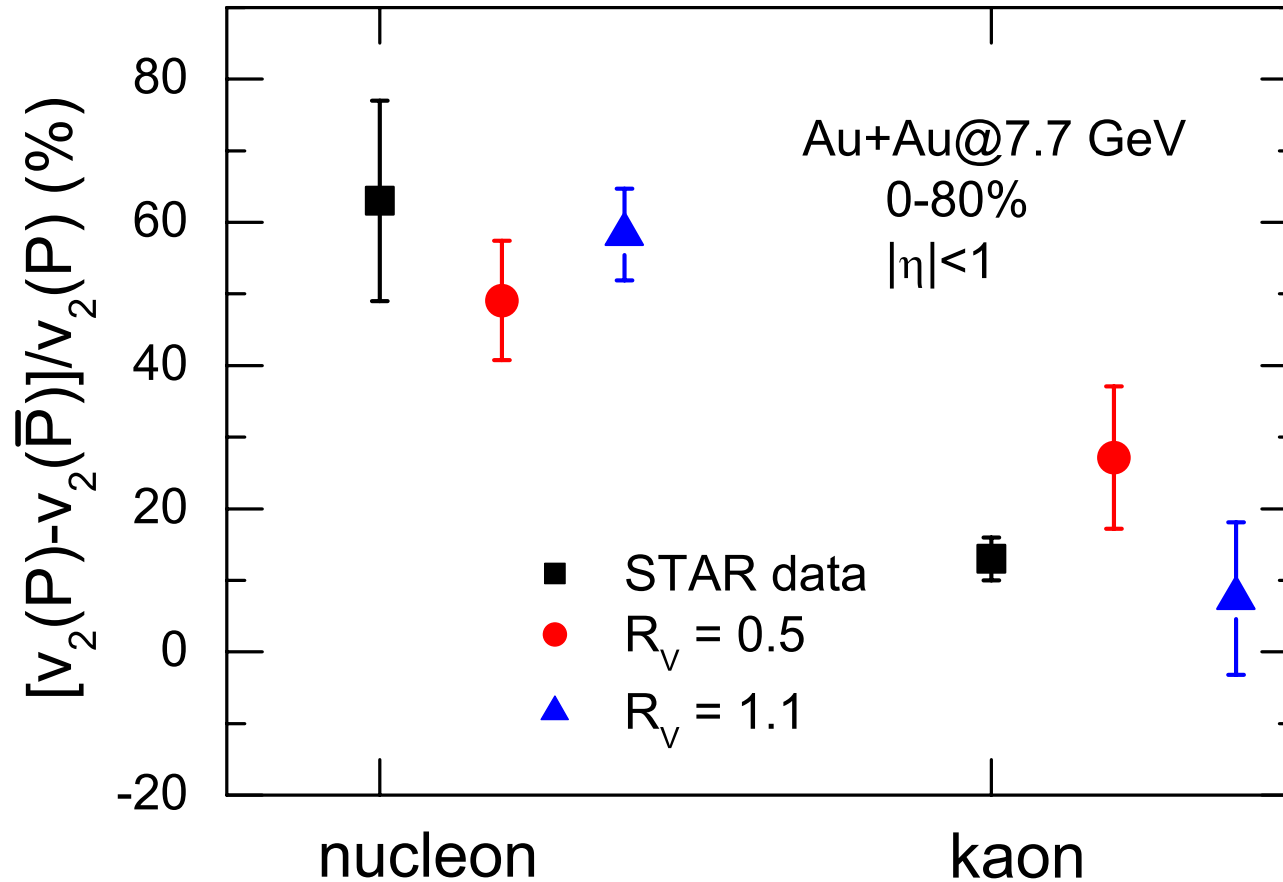
- Before hadronic evolution
 - nucleons have larger v_2 than antinucleons
 - K^- have larger v_2 than K^+
- After hadronic evolution
 - v_2 increases for all hadrons
 - v_2 of nucleons remains larger than that of antinucleons
 - v_2 of K^+ becomes larger than that of K^-

Charged hadron elliptic flow



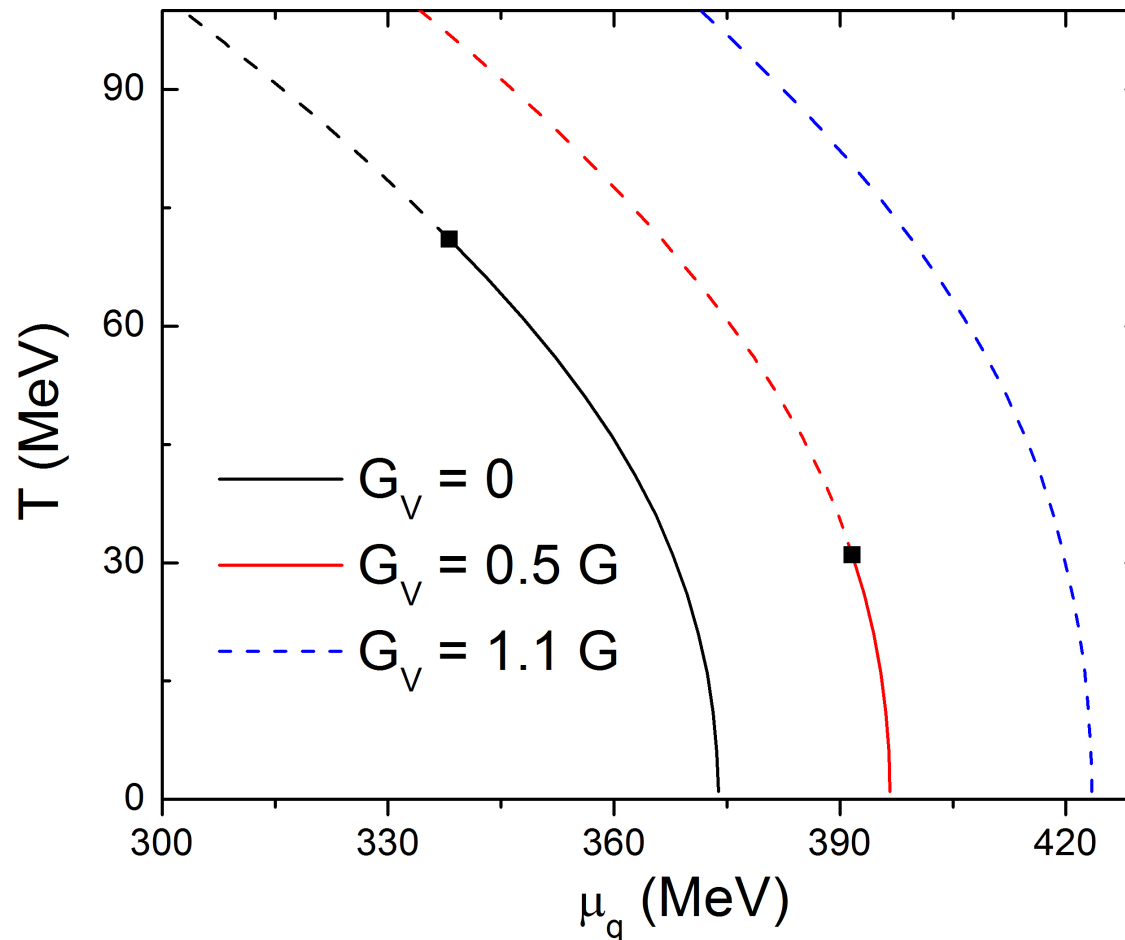
- Sensitive to parton cross section \rightarrow 1 mb to reproduce data
- Insensitive to partonic vector mean fields

Relative v_2 difference including both partonic and hadronic potentials



- Finite partonic vector mean field with $G_V/G=0.5 - 1.1$ is needed to describe STAR data

Effects of vector interaction on QCD phase diagram



- Location of critical point depends strongly on G_V ; moving to lower temperature and larger baryon chemical potential as G_V increases
- Critical point disappears for $G_V > 0.6 G$

Summary

- Different particle and antiparticle v_2 is observed in BES at RHIC where produced matter has a large finite baryon chemical potential (~ 400 MeV)
- Taking into account different potentials for hadrons and antihadrons can partially account for the experimental observation
- Quarks and antiquarks are affected by scalar and vector potentials in QGP
 - reduced v_2 due to attractive scalar potential
 - vector potential becomes nonzero at finite baryon chemical potential; repulsive for quarks and attractive for antiquarks
 - larger quark than antiquark v_2 in baryon-rich QGP
 - larger v_2 for proton than antiproton, lambda than antilambda, and K^+ than K^- (small G_V) or K^- than K^+ (large G_V) after hadronization
- Including both partonic and hadronic potentials $\rightarrow G_V = 0.5 - 1.1$ G
 \rightarrow absence of critical point in QCD phase diagram?
- Information on quark and antiquark potentials at finite baryon chemical potential is useful for understanding the phase structure of QCD