



**FIAS** Frankfurt Institute  
for Advanced Studies



**HIC**  
for **FAIR**  
Helmholtz International Center

**GOETHE**  
**UNIVERSITÄT**  
FRANKFURT AM MAIN

# **Dynamical description of strongly interacting parton-hadron matter**

**Elena Bratkovskaya**

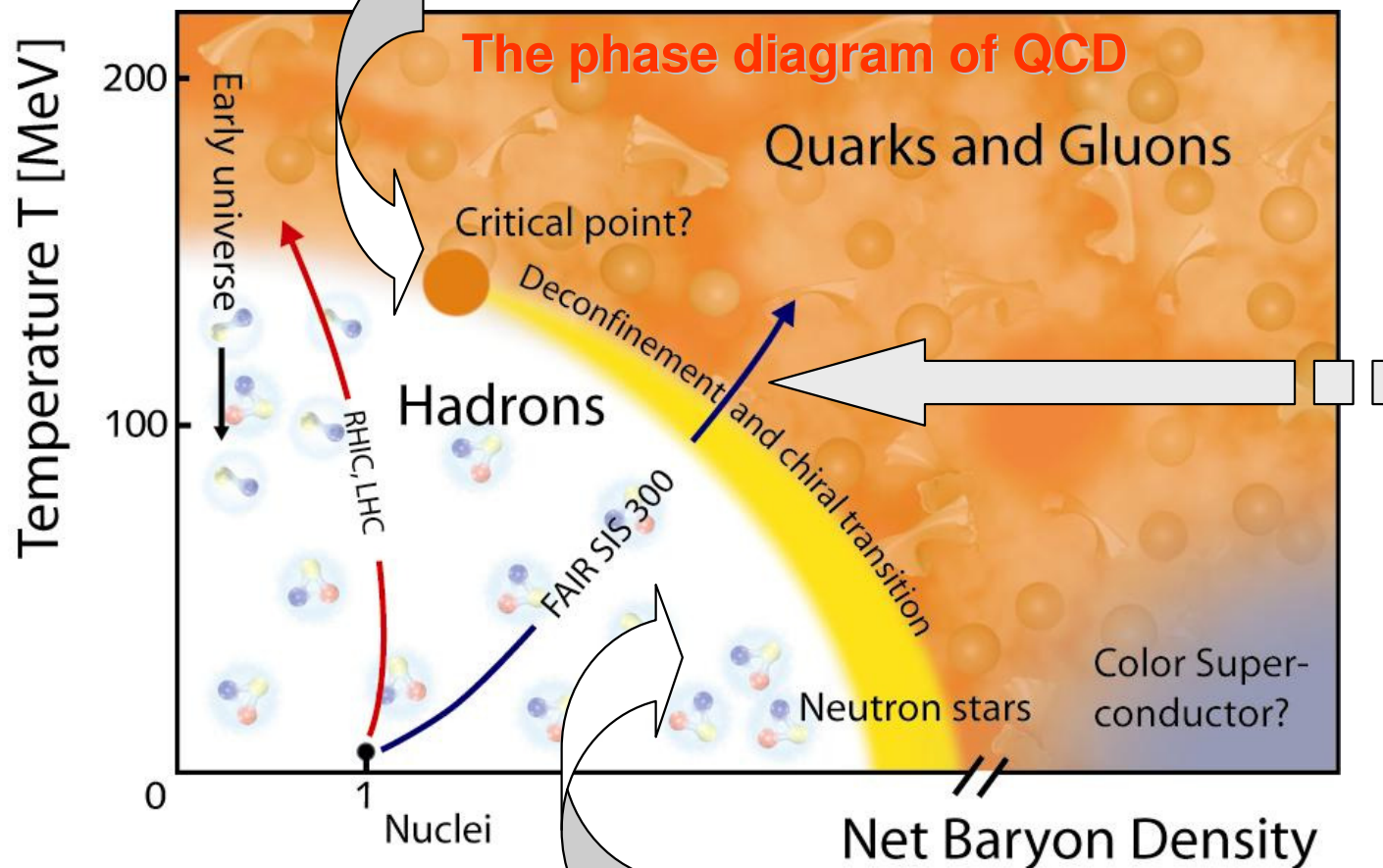
**Institut für Theoretische Physik & FIAS, Uni. Frankfurt**



*The 9th Relativistic Aspects of Nuclear Physics workshop  
(RANP2013), September 23 to 27, 2013, Rio de Janeiro, Brazil*

# The holy grail of heavy-ion physics:

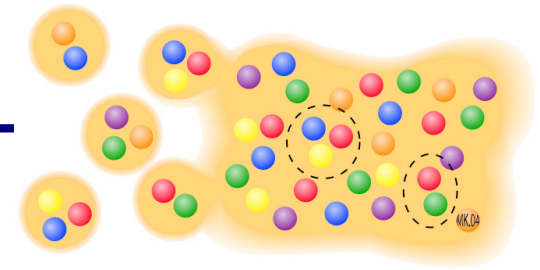
- Search for the **critical point**



- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**

- Study of the **in-medium** properties of hadrons at high baryon density and temperature

# From hadrons to partons



In order to study the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma** – we **need a consistent non-equilibrium (transport) model with**

- **explicit parton-parton interactions** (i.e. between quarks and gluons) beyond strings!

- **explicit phase transition** from hadronic to partonic degrees of freedom
- **IQCD EoS** for partonic phase

**Transport theory:** off-shell Kadanoff-Baym equations for the Green-functions  $S_h^<(x,p)$  in phase-space representation for the **partonic and hadronic phase**



**Parton-Hadron-String-Dynamics (PHSD)**

**QGP phase** described by

**Dynamical QuasiParticle Model (DQPM)**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215;  
W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

# Dynamical QuasiParticle Model (DQPM) - Basic ideas:

DQPM describes QCD properties in terms of ,resummed‘ single-particle Green’s functions – in the sense of a two-particle irreducible (2PI) approach:

Gluon propagator:  $\Delta^{-1} = P^2 - \Pi$

gluon self-energy:  $\Pi = M_g^2 - i2\Gamma_g \omega$

Quark propagator:  $S_q^{-1} = P^2 - \Sigma_q$

quark self-energy:  $\Sigma_q = M_q^2 - i2\Gamma_q \omega$

- the resummed properties are specified by complex self-energies which depend on temperature:
  - the real part of self-energies ( $\Sigma_q, \Pi$ ) describes a **dynamically generated mass** ( $M_q, M_g$ );
  - the imaginary part describes the **interaction width** of partons ( $\Gamma_q, \Gamma_g$ )
- space-like part of energy-momentum tensor  $T_{\mu\nu}$  defines the potential energy density and the **mean-field potential** (1PI) for quarks and gluons
- 2PI framework guaranties a consistent description of the system **in- and out-off equilibrium** on the basis of Kadanoff-Baym equations



# The Dynamical QuasiParticle Model (DQPM)

**Properties** of interacting quasi-particles: massive quarks and gluons ( $g, q, q_{\text{bar}}$ ) with Lorentzian spectral functions :

$$\rho_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{\left(\omega^2 - \bar{p}^2 - M_i^2(T)\right)^2 + 4\omega^2\Gamma_i^2(T)}$$

$(i = q, \bar{q}, g)$

■ Modeling of the quark/gluon masses and widths → HTL limit at high T

■ **quarks:**

**mass:**  $M_{q(\bar{q})}^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left( T^2 + \frac{\mu_q^2}{\pi^2} \right)$

**width:**  $\Gamma_{q(\bar{q})}(T) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$

■ **gluons:**

$$M_g^2(T) = \frac{g^2}{6} \left( \left( N_c + \frac{N_f}{2} \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$\Gamma_g(T) = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$

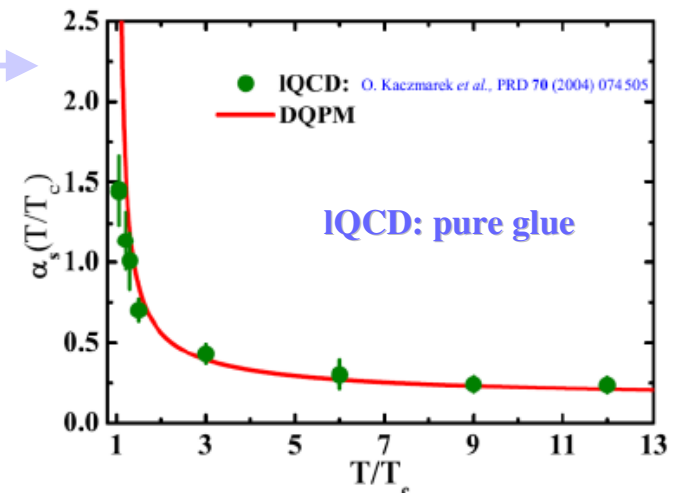
$N_c = 3, N_f = 3$

■ **running coupling (pure glue):**

$$\alpha_s(T) = \frac{g^2(T)}{4\pi} = \frac{12\pi}{(11N_c - 2N_f) \ln[\lambda^2(T/T_c - T_s/T_c)^2]}$$

□ **fit to lattice (IQCD) results (e.g. entropy density)**

with 3 parameters:  $T_s/T_c = 0.46$ ;  $c = 28.8$ ;  $\lambda = 2.42$   
(for pure glue  $N_f = 0$ )



DQPM: Peshier, Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

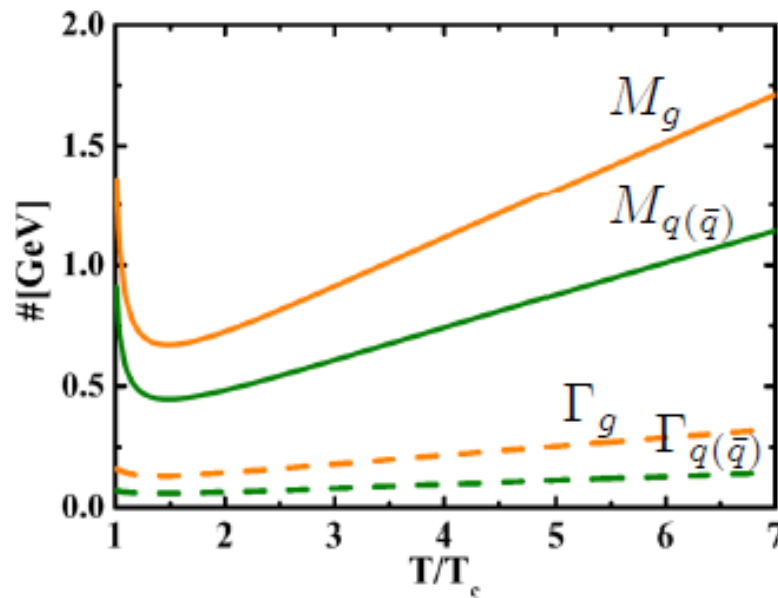
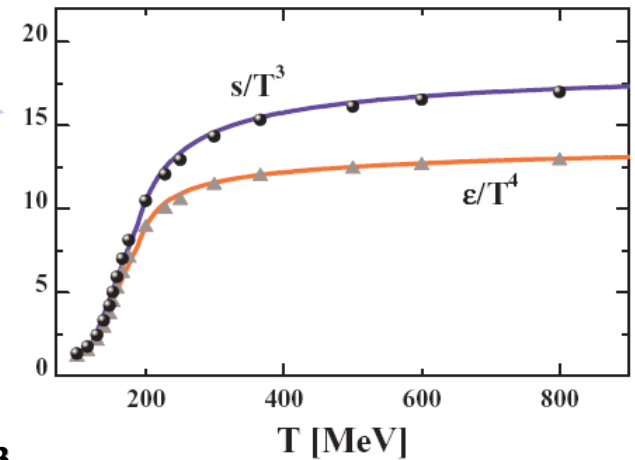
# The Dynamical QuasiParticle Model (DQPM)

➤ **fit to lattice (IQCD) results** (e.g. entropy density)

\* BMW IQCD data S. Borsanyi et al., JHEP 1009 (2010) 073

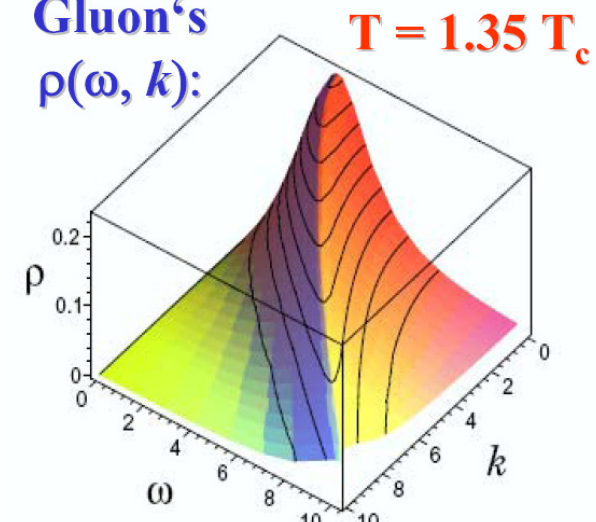
➔ **Quasiparticle properties:**

■ **large width and mass for gluons and quarks**



$T_C = 158 \text{ MeV}$   
 $\epsilon_C = 0.5 \text{ GeV/fm}^3$

Gluon's  
 $\rho(\omega, k):$



Plot from Peshier,  
 PRD 70 (2004)  
 034016

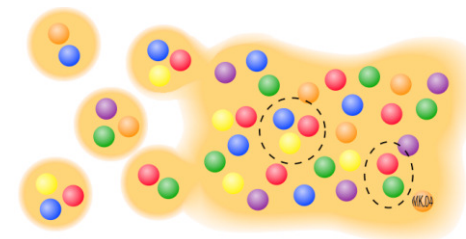
- **DQPM matches well lattice QCD**
- **DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)**
- **DQPM gives transition rates for the formation of hadrons → PHSD**



# I. PHSD - basic concept

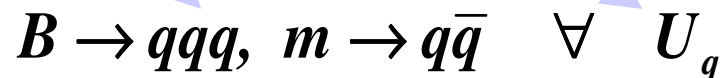
## I. From hadrons to QGP:

- **Initial A+A collisions** – as in HSD:
  - **string** formation in primary NN collisions
  - string decay to **pre-hadrons** ( $B$  - baryons,  $m$  - mesons)



- **Formation of QGP stage** by dissolution of pre-hadrons (all new produced secondary hadrons) into **massive colored quarks + mean-field energy**

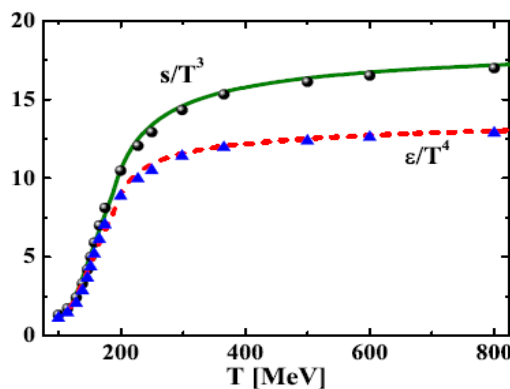
**QGP phase:**  
 $\epsilon > \epsilon_{\text{critical}}$



based on the **Dynamical Quasi-Particle Model (DQPM)** which defines **quark spectral functions**, i.e. masses  $M_q(\epsilon)$  and widths  $\Gamma_q(\epsilon)$

+ **mean-field potential  $U_q$**  at given  $\epsilon$  – local energy density

( $\epsilon$  related by IQCD EoS to  $T$  - temperature in the local cell)



W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215; EPJ ST 168 (2009) 3; NPA856 (2011) 162.



# II. PHSD - basic concept

## II. Partonic phase - QGP:

quarks and gluons (= ‚dynamical quasiparticles‘)

with off-shell spectral functions (width, mass) defined by the DQPM

- in **self-generated mean-field potential** for quarks and gluons  $U_q, U_g$  from the DQPM
- **EoS of partonic phase: ‚crossover‘** from lattice QCD (fitted by DQPM)
- **(quasi-) elastic and inelastic** parton-parton interactions: using the effective cross sections from the DQPM

- **(quasi-) elastic collisions:**

$$q + q \rightarrow q + q \quad g + q \rightarrow g + q$$

$$q + \bar{q} \rightarrow q + \bar{q} \quad g + \bar{q} \rightarrow g + \bar{q}$$

$$\bar{q} + \bar{q} \rightarrow \bar{q} + \bar{q} \quad g + g \rightarrow g + g$$

- **inelastic collisions:**

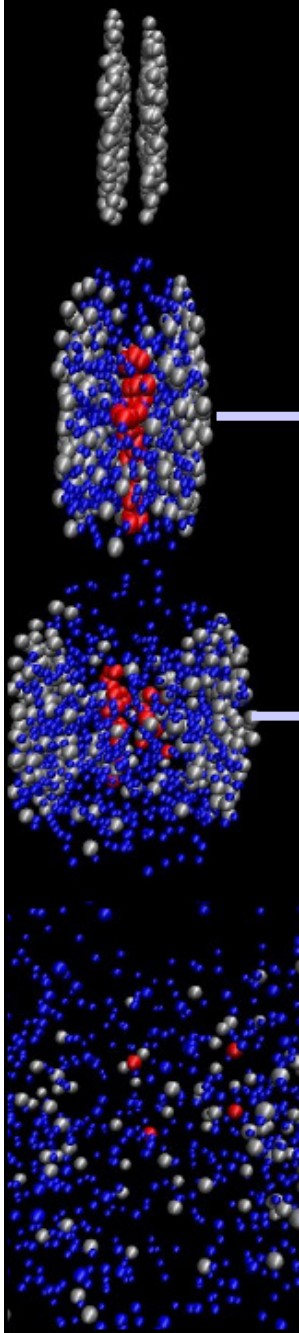
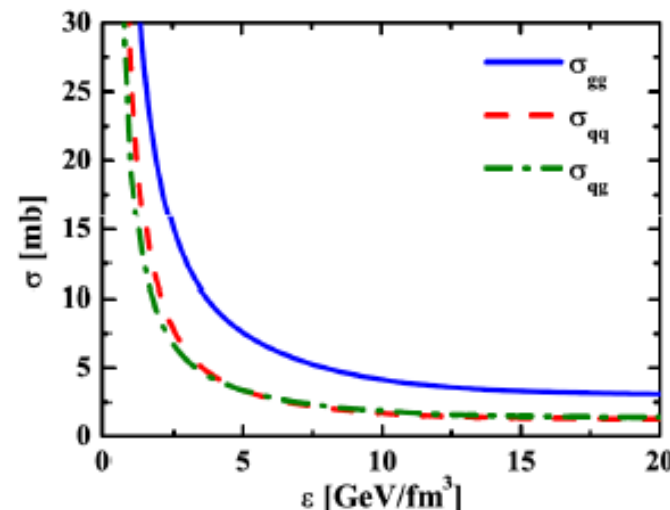
(Breight-Wigner cross sections)



$$\left\{ \begin{array}{l} q + \bar{q} \rightarrow g \\ g \rightarrow q + \bar{q} \end{array} \right.$$

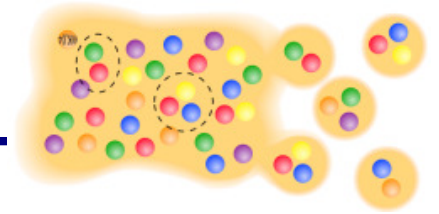
$$\left\{ \begin{array}{l} q + \bar{q} \rightarrow g + g \\ g \rightarrow g + g \end{array} \right.$$

suppressed (<1%)  
due to the large  
mass of gluons





# III. PHSD - basic concept



## III. Hadronization:

□ **Hadronization:** based on DQPM

- **massive, off-shell (anti-)quarks** with broad spectral functions hadronize to **off-shell mesons and baryons or color neutral excited states - ,strings‘** (strings act as ,doorway states‘ for hadrons)

$$g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow \text{meson ('string' )}$$

$$q + q + q \leftrightarrow \text{baryon ('string' )}$$

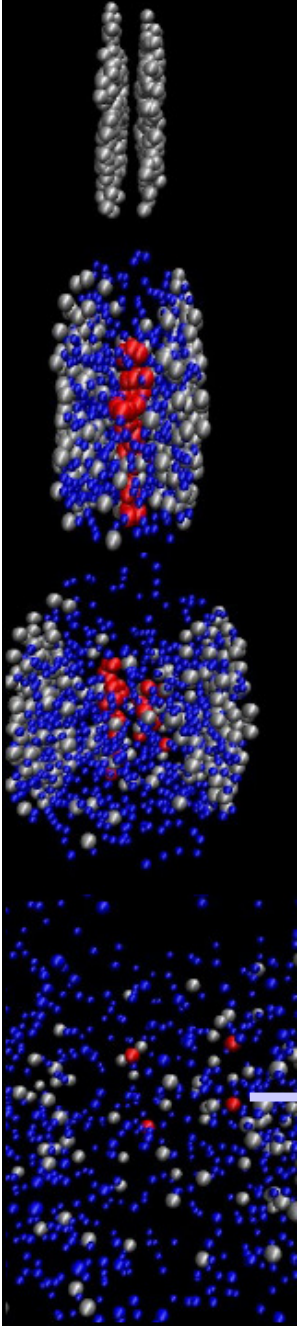
- Local covariant off-shell **transition rate** for q+qbar fusion  
 → **meson formation:**

$$\frac{dN^{q+\bar{q} \rightarrow m}}{d^4x d^4p} = \text{Tr}_q \text{Tr}_{\bar{q}} \delta^4(p - p_q - p_{\bar{q}}) \delta^4\left(\frac{x_q + x_{\bar{q}}}{2} - x\right) \delta(\text{flavor, color})$$

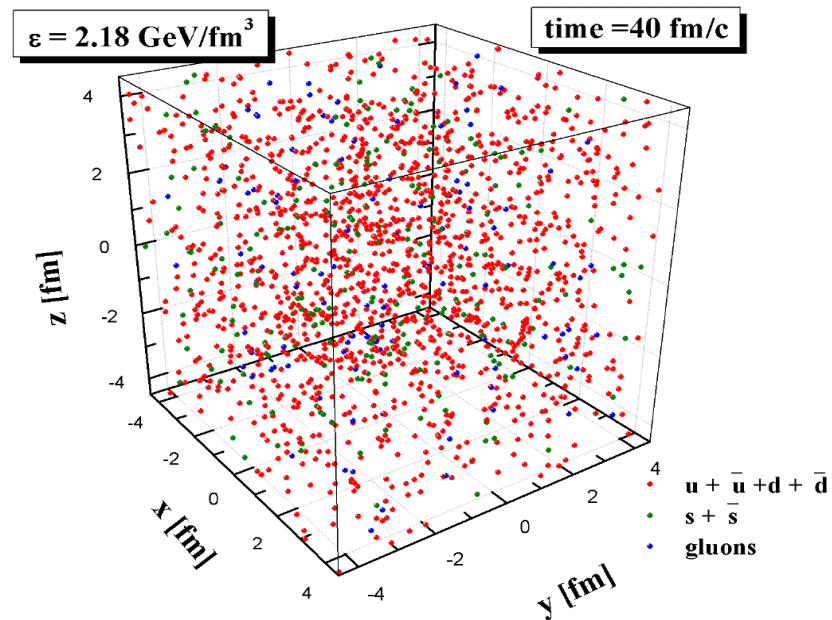
$$\cdot N_q(x_q, p_q) N_{\bar{q}}(x_{\bar{q}}, p_{\bar{q}}) \cdot \omega_q \rho_q(p_q) \cdot \omega_{\bar{q}} \rho_{\bar{q}}(p_{\bar{q}}) \cdot |M_{q\bar{q}}|^2 \underline{W_m(x_q - x_{\bar{q}}, p_q - p_{\bar{q}})}$$

- $N_j(x,p)$  is the phase-space density of parton j at space-time position x and 4-momentum p
- $W_m$  is the phase-space distribution of the formed ,pre-hadrons‘ (Gaussian in phase space)
- $|M_{q\bar{q}}|^2$  is the effective quark-antiquark interaction from the DQPM

## IV. Hadronic phase: hadron-string interactions – off-shell HSD



# Properties of the QGP in-equilibrium using PHSD







# Properties of parton-hadron matter in equilibrium

V. Ozvenchuk et al., PRC 87 (2013) 024901, arXiv:1203.4734

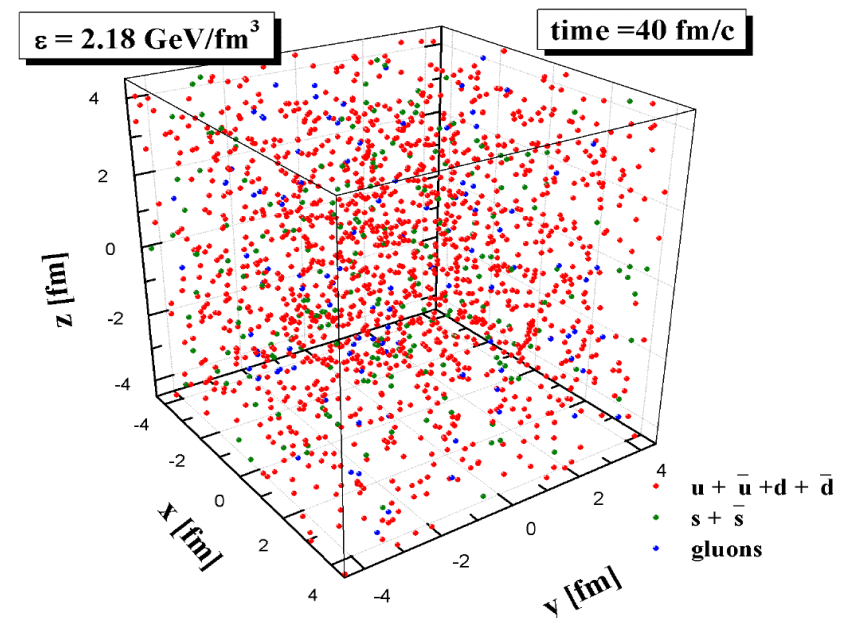
V. Ozvenchuk et al., PRC 87 (2013) 064903, arXiv:1212.5393

## The goal:

- ❑ **study of the dynamical equilibration** of QGP within the non-equilibrium off-shell PHSD transport approach
- ❑ **transport coefficients** (shear and bulk viscosities) of strongly interacting partonic matter in equilibrium
- ❑ particle number **fluctuations** (scaled variance, skewness, kurtosis)

## Realization:

- ❑ Initialize the system in a **finite box with periodic boundary conditions** with some energy density  $\varepsilon$  and chemical potential  $\mu_q$
- ❑ Evolve the system in time until equilibrium is achieved





# Properties of parton-hadron matter – shear viscosity

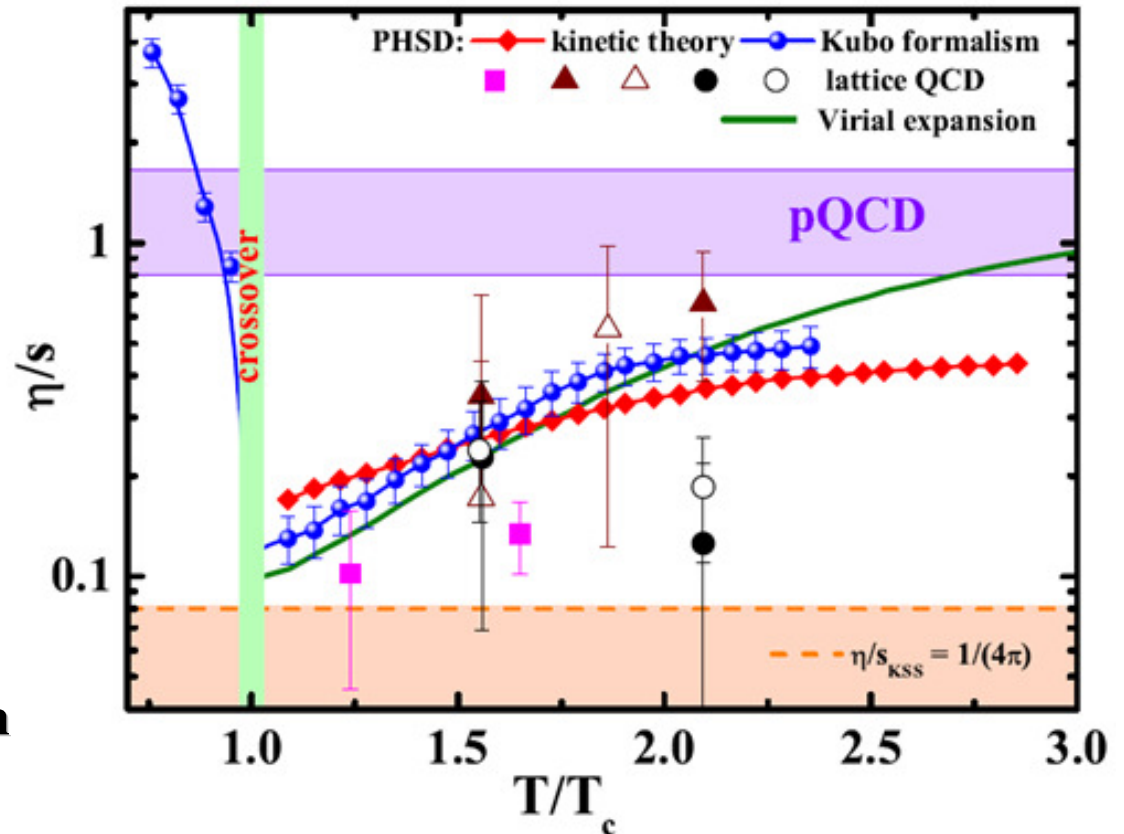
$\eta/s$  using Kubo formalism and the relaxation time approximation (,kinetic theory‘)

□  $T=T_c$ :  $\eta/s$  shows a minimum ( $\sim 0.1$ ) close to the critical temperature

□  $T>T_c$ : QGP - pQCD limit at higher temperatures  $T > 3 T_c$

□  $T<T_c$ : fast increase of the ratio  $\eta/s$  for hadronic matter →

- lower interaction rate of hadronic system
- smaller number of degrees of freedom (or entropy density) for hadronic matter compared to the QGP



Virial expansion: S. Mattiello, W. Cassing, Eur. Phys. J. C 70, 243 (2010).

**QGP in PHSD = strongly-interacting liquid**

# Transport coefficients from (P)NJL: shear viscosity

R. Marty, E.B., W. Cassing, J. Aichelin, H. Berrehrah, arXiv:1305.7180 [hep-ph]

- **NJL SU(3)<sub>f</sub> model** (from Nantes group)

$$\mathcal{L}_{NJL} = \bar{\psi} (i\cancel{\partial} - m_0) \psi + G \sum_{a=0}^8 \left[ (\bar{\psi} \lambda^a \psi)^2 + (\bar{\psi} i \gamma_5 \lambda^a \psi)^2 \right] - K [\det \bar{\psi} (1 - \gamma_5) \psi + \det \bar{\psi} (1 + \gamma_5) \psi]$$

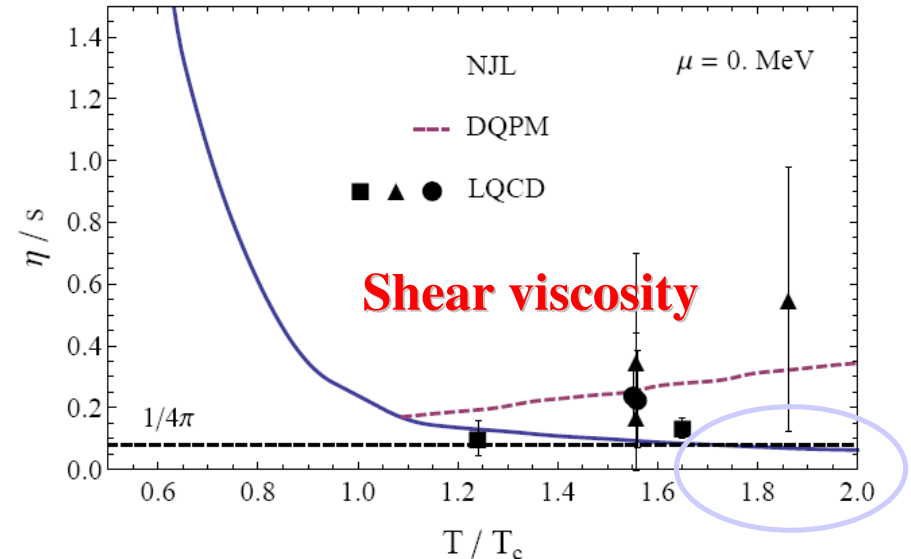
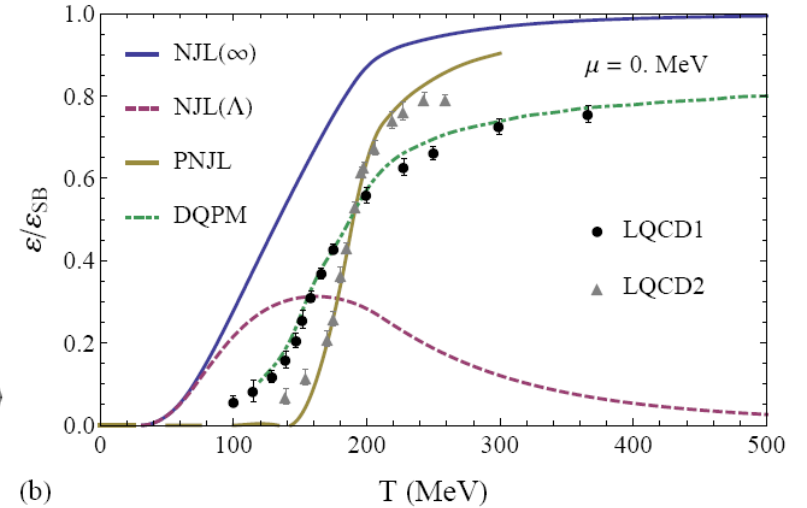
- **masses:**  $m_i = m_{0i} - 4G \langle \bar{\psi}_i \psi_i \rangle + 2K \langle \bar{\psi}_j \psi_j \rangle \langle \bar{\psi}_k \psi_k \rangle$

- **quark condensate in the mean field limit:**

$$\langle \bar{\psi}_i \psi_i \rangle = -2N_c \int_0^\Lambda \frac{d^3 p}{(2\pi)^3} \frac{m_i}{E_{ip}} [1 - f_q - f_{\bar{q}}]$$

- **NJL:  $\eta/s < 1/4\pi$  for  $T > 1.7 T_c$**
- ➔ **the applicability of the NJL model should be restricted to temperatures at least below  $1.7 T_c$**

**NJL:  $T_c = T_{\text{Mott}} = 200 \text{ MeV}$**



LQCD1: S. Borsanyi, G. Endrodi, Z. Fodor, A. Jakovac, S. D. Katz, et al., JHEP 1011, 077 (2010)  
 LQCD2: M. Cheng, S. Ejiri, P. Hegde, F. Karsch, O. Kaczmarek, et al., Phys. Rev. D 81, 054504 (2010)  
 PNJL: P. Costa, M. Ruivo, C. de Sousa, and H. Hansen, Symmetry 2, 1338 (2010)



# Bulk viscosity (mean-field effects)

□ bulk viscosity in relaxation time approximation with **mean-field** effects:

Chakraborty, Kapusta, Phys. Rev.C 83, 014906 (2011).

$$\zeta = \frac{1}{TV} \sum_{i=1}^N \frac{\Gamma_i^{-1}}{E_i^2} \left[ \left( \frac{1}{3} - v_s^2 \right) |\mathbf{p}|^2 - v_s^2 \left( m_i^2 - T^2 \frac{dm_i^2}{dT^2} \right) \right]^2$$

use DQPM results for masses for  $\mu_q=0$ :

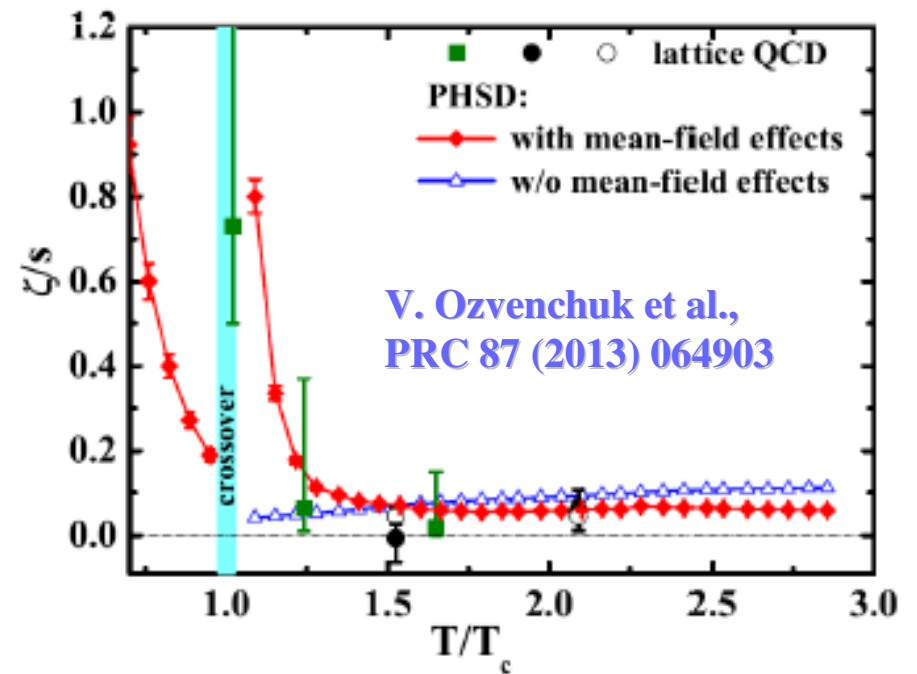
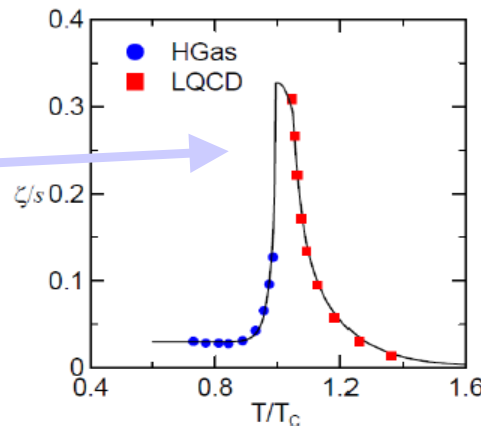
$$m_q^2 = \frac{1}{3} g^2 T^2, \quad m_g^2 = \frac{3}{4} g^2 T^2$$

**PHSD** using the relaxation time approximation:

□ **significant rise** in the vicinity of the critical temperature

□ **in line** with the ratio from **IQCD** calculations

Cf. talk by Gabriel Denicol

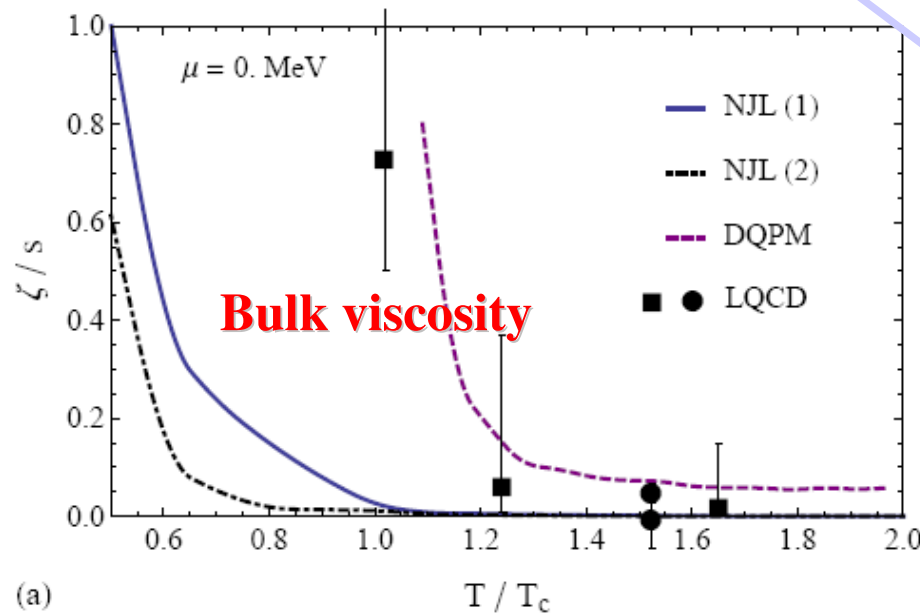


IQCD: Meyer, Phys. Rev. Lett. 100, 162001 (2008); Sakai, Nakamura, Pos LAT2007, 221 (2007).

# Transport coefficients from (P)NJL: bulk viscosity

R. Marty, E.B., W. Cassing, J. Aichelin, H. Berrehrach, arXiv:1305.7180 [hep-ph]

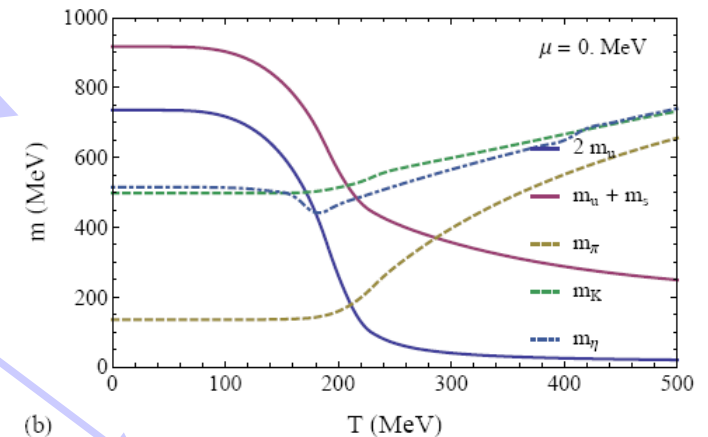
$$\zeta = \frac{1}{TV} \sum_{i=1}^N \frac{\Gamma_i^{-1}}{E_i^2} \left[ \left( \frac{1}{3} - v_s^2 \right) |\mathbf{p}|^2 - v_s^2 \left( m_i^2 - T^2 \frac{dm_i^2}{dT^2} \right) \right]^2$$



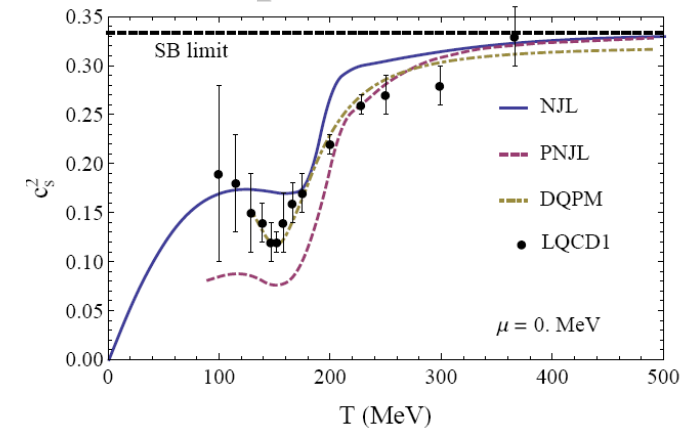
NJL (1): NJL using the RTA method Chakraborty, Kapusta, Phys. Rev.C 83, 014906 (2011)

NJL (2): NJL model with method from Sasaki, Redlich, Phys.Rev. C79, 055207 (2009)

## masses in NJL



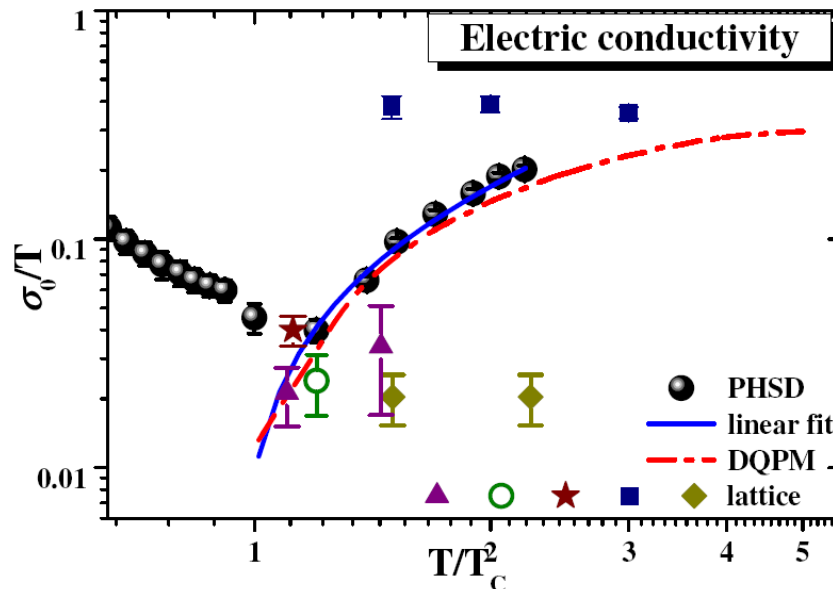
## Speed of sound



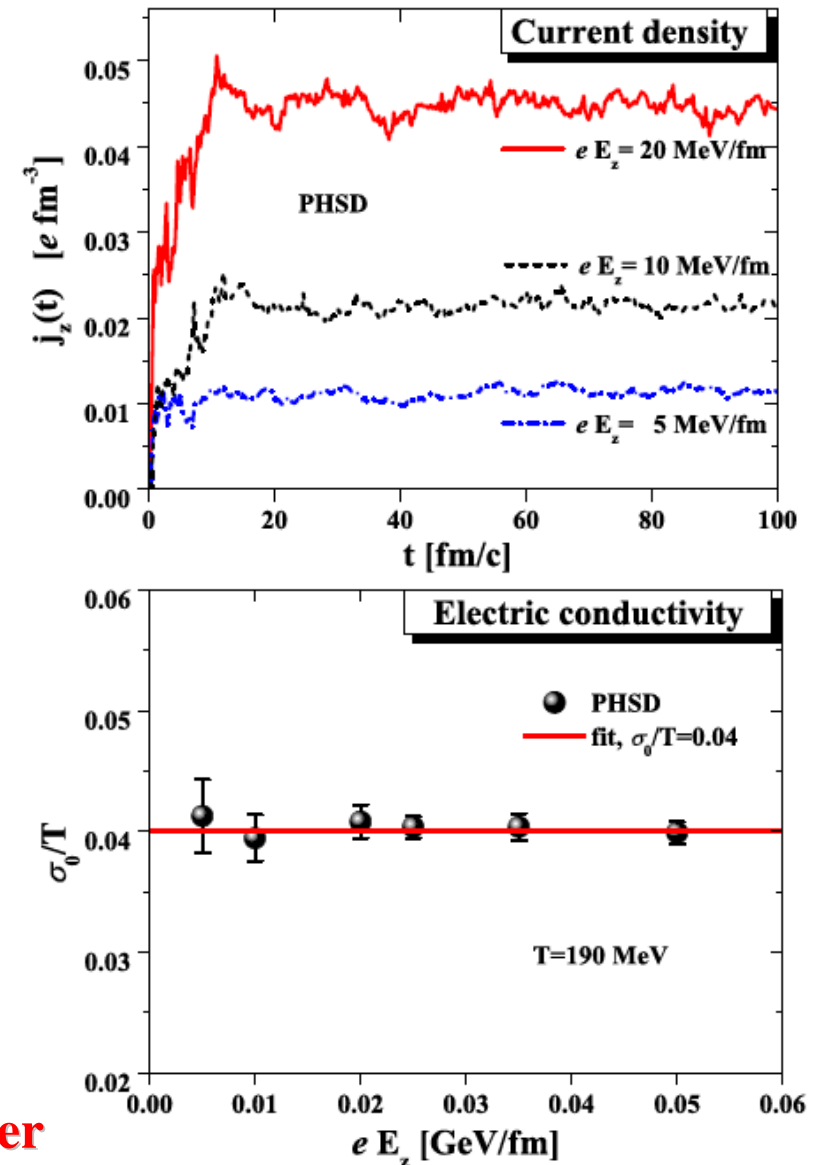
$\zeta/s$  from NJL is not consistent with the available LQCD data

- The response of the strongly-interacting system in equilibrium to an external electric field  $eE_z$  defines the electric conductivity  $\sigma_0$ :

$$\frac{\sigma_0}{T} = \frac{j_{eq}}{E_z T}, \quad j_z(t) = \frac{1}{V} \sum_j e q_j \frac{p_z^j(t)}{M_j(t)}$$



- the QCD matter even at  $T \sim T_c$  is a much better electric conductor than Cu or Ag (at room temperature) by a factor of 500 !





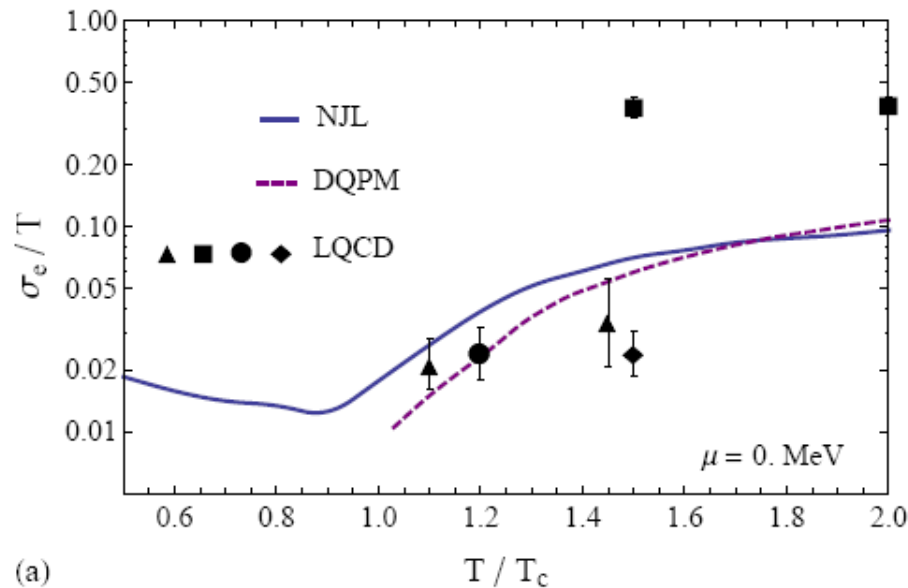
# Transport coefficients from NJL: electric and heat conductivity

R. Marty, E.B., W. Cassing, J. Aichelin, H. Berrehrach, arXiv:1305.7180 [hep-ph]

## Electric conductivity

$$\sigma_e(T, \mu) = \sum_q \frac{e_q^2 n_q(T, \mu) \tau_q(T, \mu)}{m_q(T, \mu)}$$

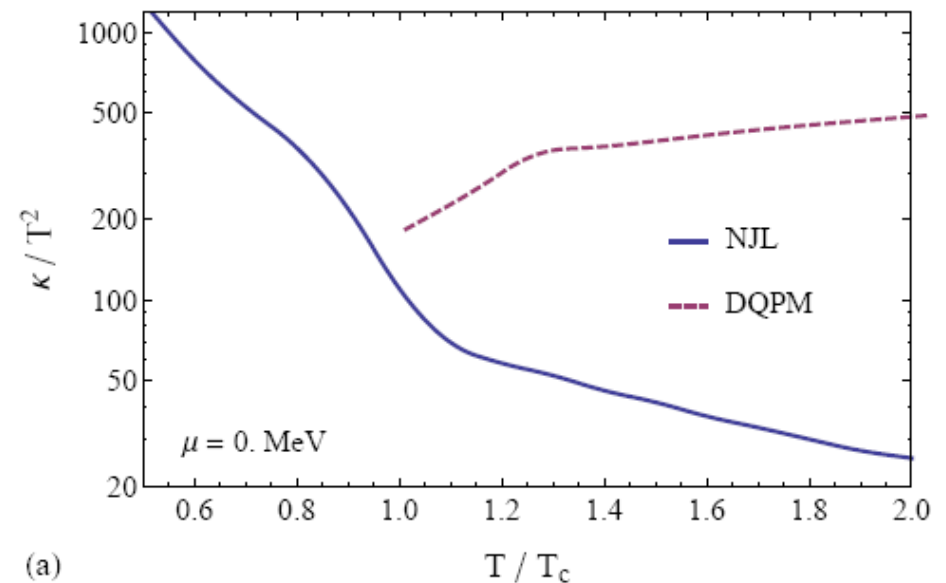
$q = u, d, s, \bar{u}, \bar{d}, \bar{s}$



## Heat conductivity

$$\kappa(T, \mu) = \frac{1}{3} v_{\text{rel}} c_V(T, \mu) \sum_f \tau_f(T, \mu)$$

specific heat      relaxation time



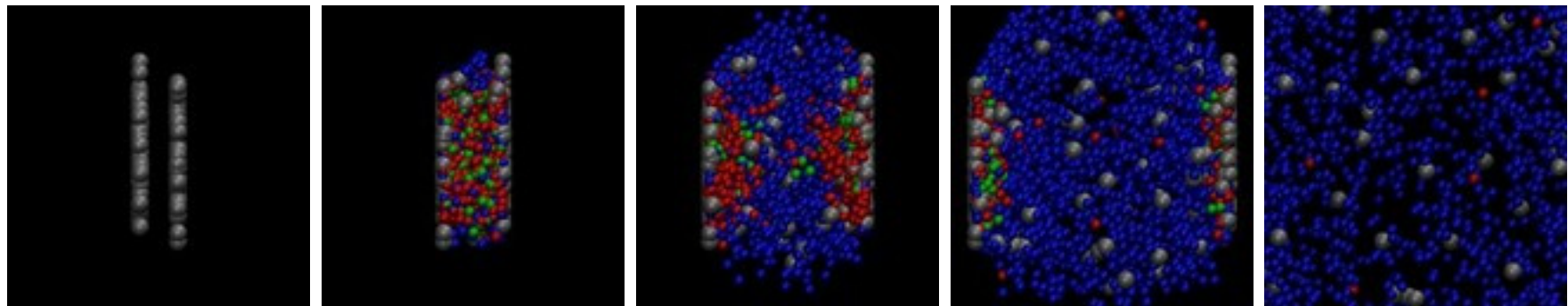
For  $T > T_c$ :

□ electric conductivity from NJL and DQPM agree roughly with LQCD

□ heat conductivity from NJL and DQPM show very different behavior

**=> LQCD data are needed !**

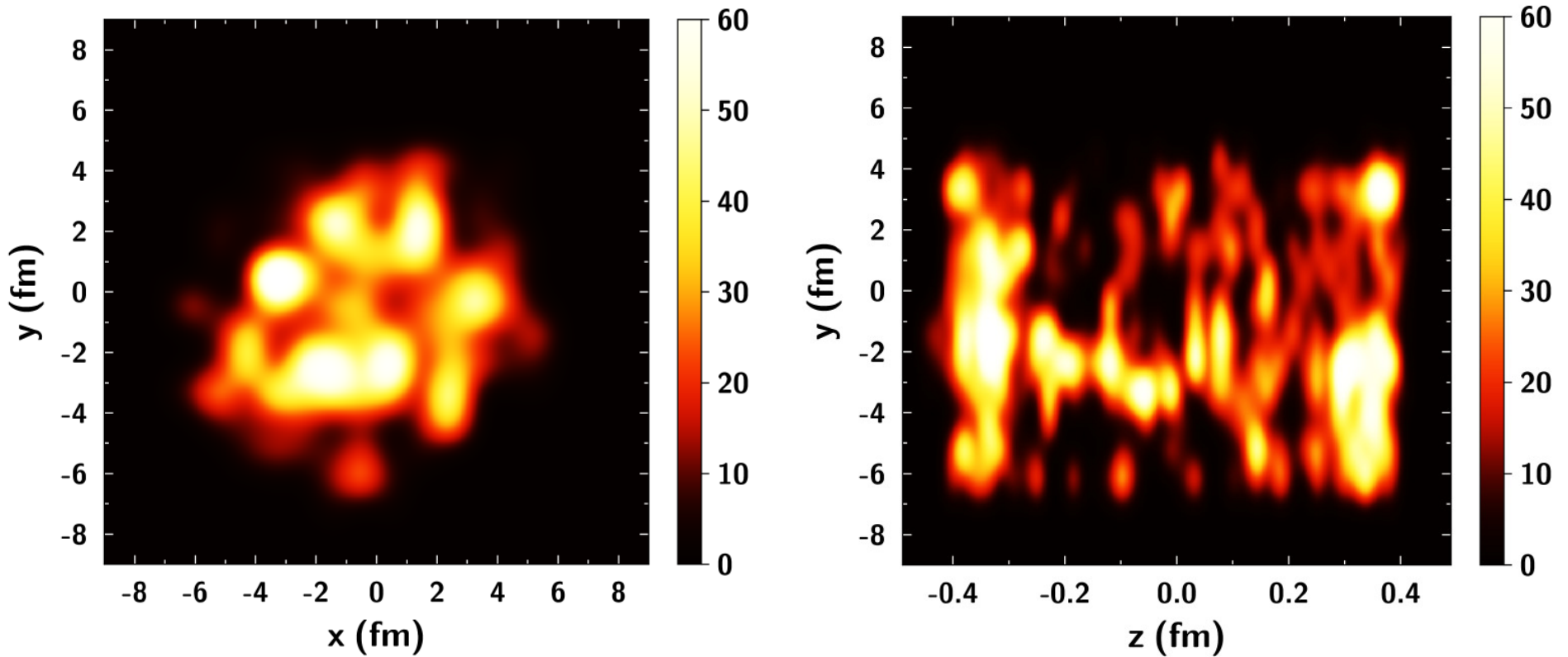
# Properties of the QGP out-of-equilibrium using PHSD





# PHSD for HIC

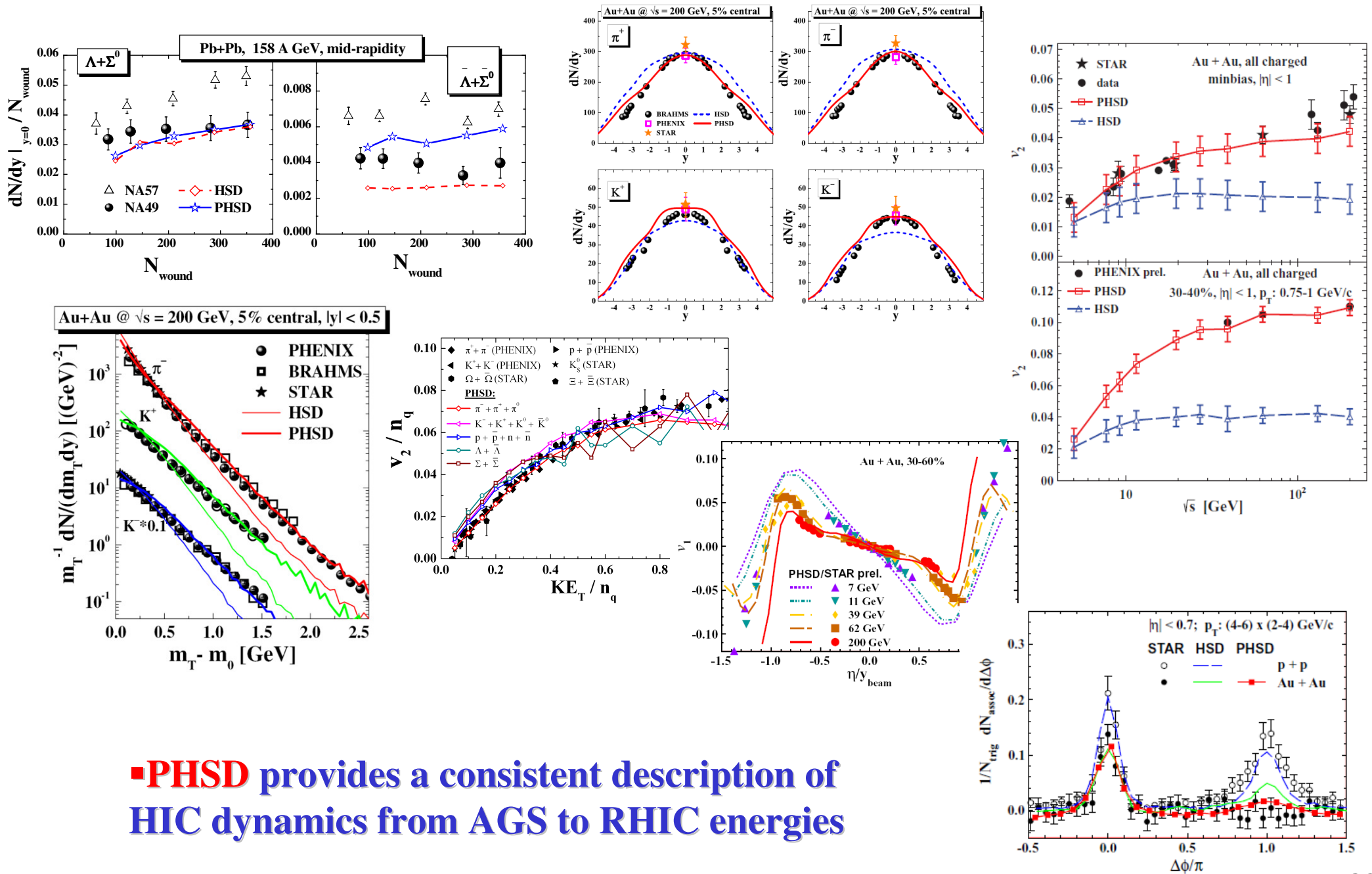
Energy density  $\epsilon(\text{GeV}/\text{fm}^2)$  for Au+Au at  $s^{1/2} = 200 \text{ GeV}$   
with impact parameter  $b = 2 \text{ fm}$  in the rest frame



Fluctuating energy density  $\epsilon(\text{GeV}/\text{fm}^3)$  in PHSD



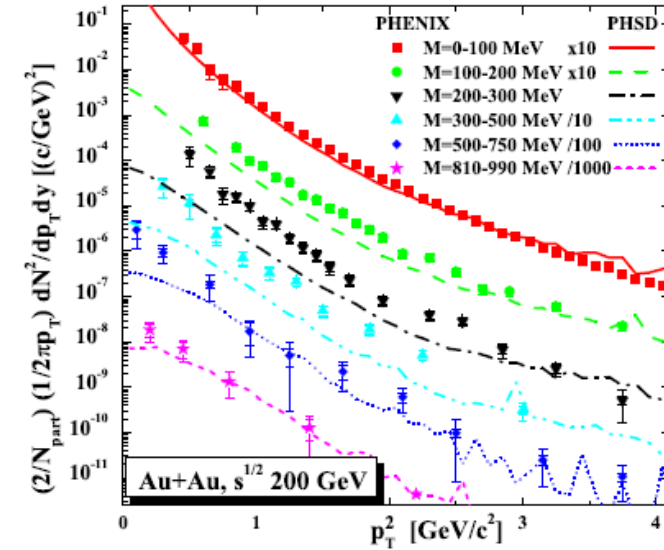
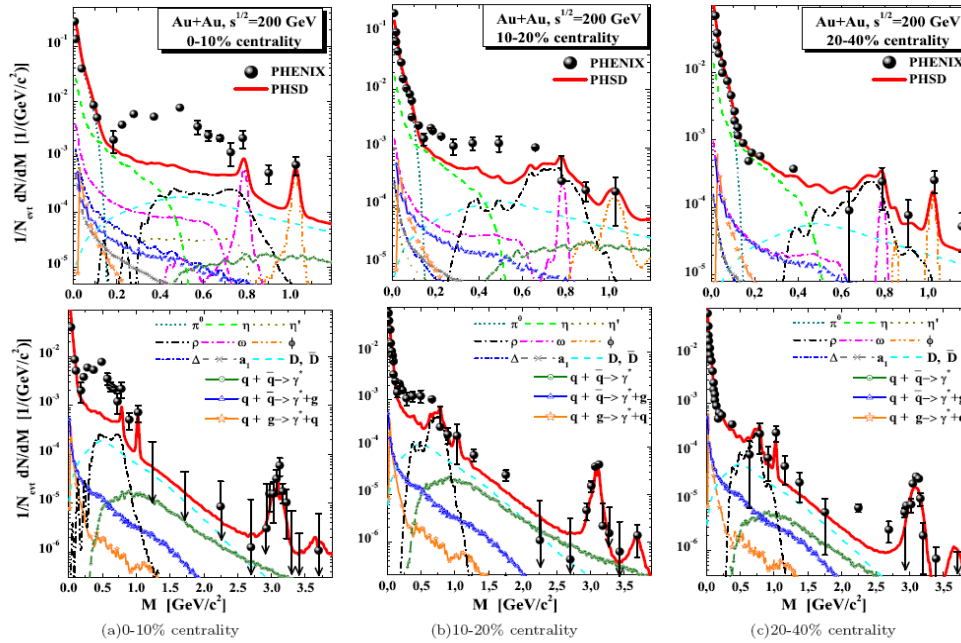
# PHSD for HIC (highlights)



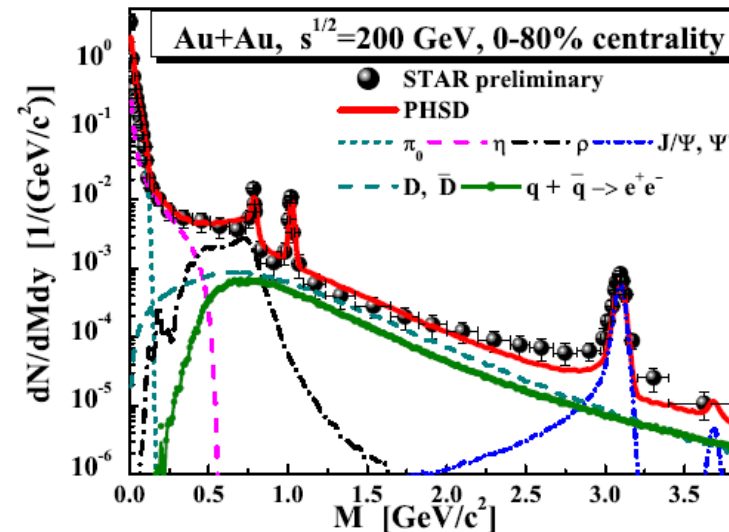
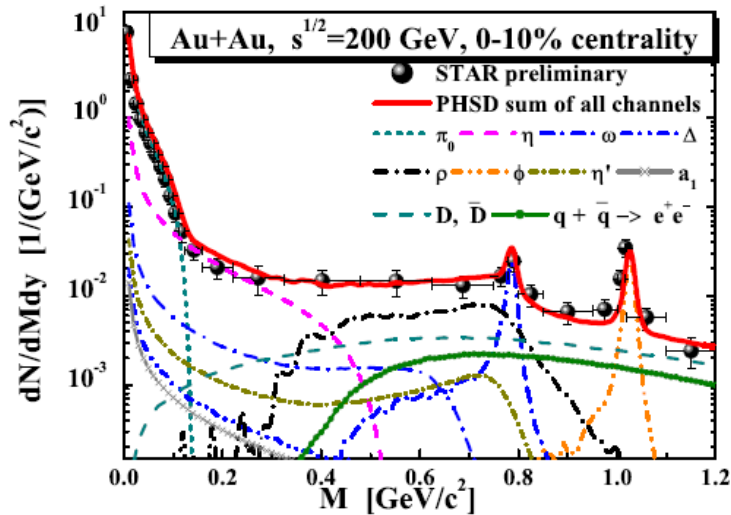
■ **PHSD** provides a consistent description of HIC dynamics from AGS to RHIC energies



# PHENIX, STAR dilepton spectra



■ **PHENIX: Peripheral collisions (and pp) are well described, however, central fail!**



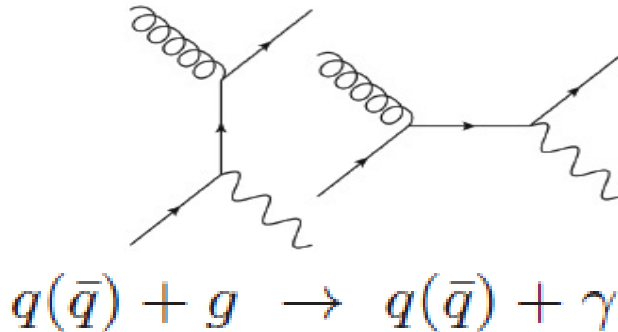
■ **STAR data are well described!**

# Photons from the hot and dense medium

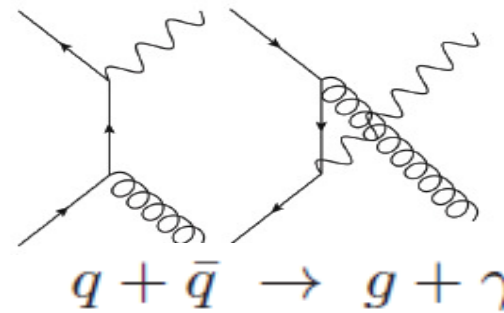
□ from the **QGP** via **partonic interactions**:

## Photon sources:

**Compton scattering**



**q-qbar annihilation**



□ from **hadronic sources**:

• **decays of mesons:**  $\pi \rightarrow \gamma + \gamma, \eta \rightarrow \gamma + \gamma, \omega \rightarrow \pi + \gamma$   
 $\eta' \rightarrow \rho + \gamma, \phi \rightarrow \eta + \gamma, a_1 \rightarrow \pi + \gamma$

• **secondary meson interactions:**  $\pi + \pi \rightarrow \rho + \gamma, \rho + \pi \rightarrow \pi + \gamma$

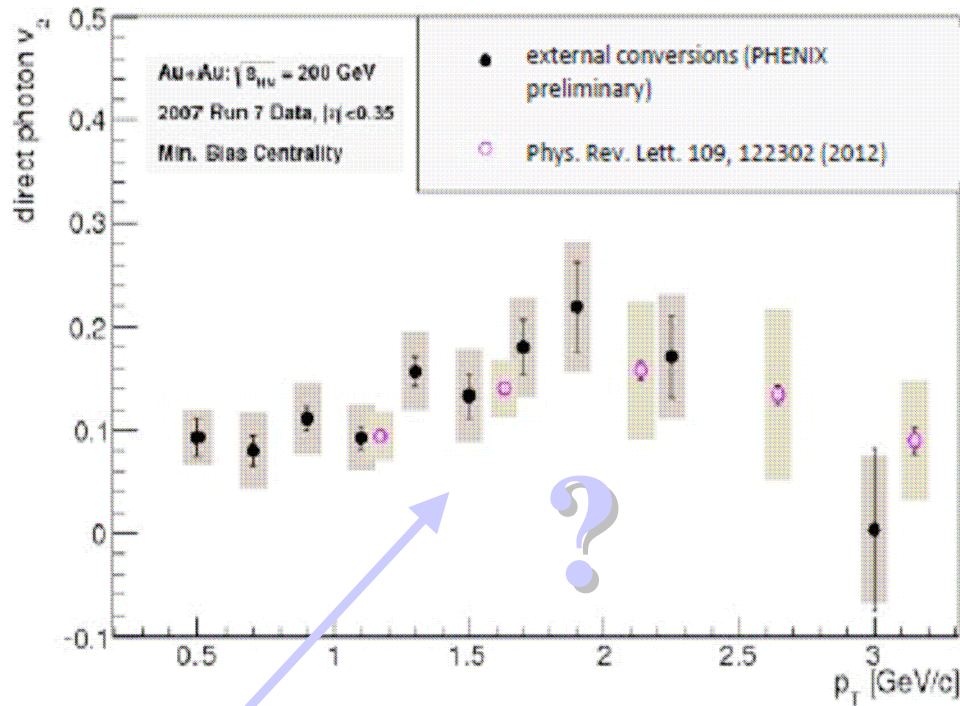
using the off-shell extension of Kapusta et al. in PRD44 (1991) 2774

• **meson-meson bremsstrahlung:**  $m+m \rightarrow m+m+\gamma, m=\pi,\eta,\rho,\omega,K,K^*,\dots$

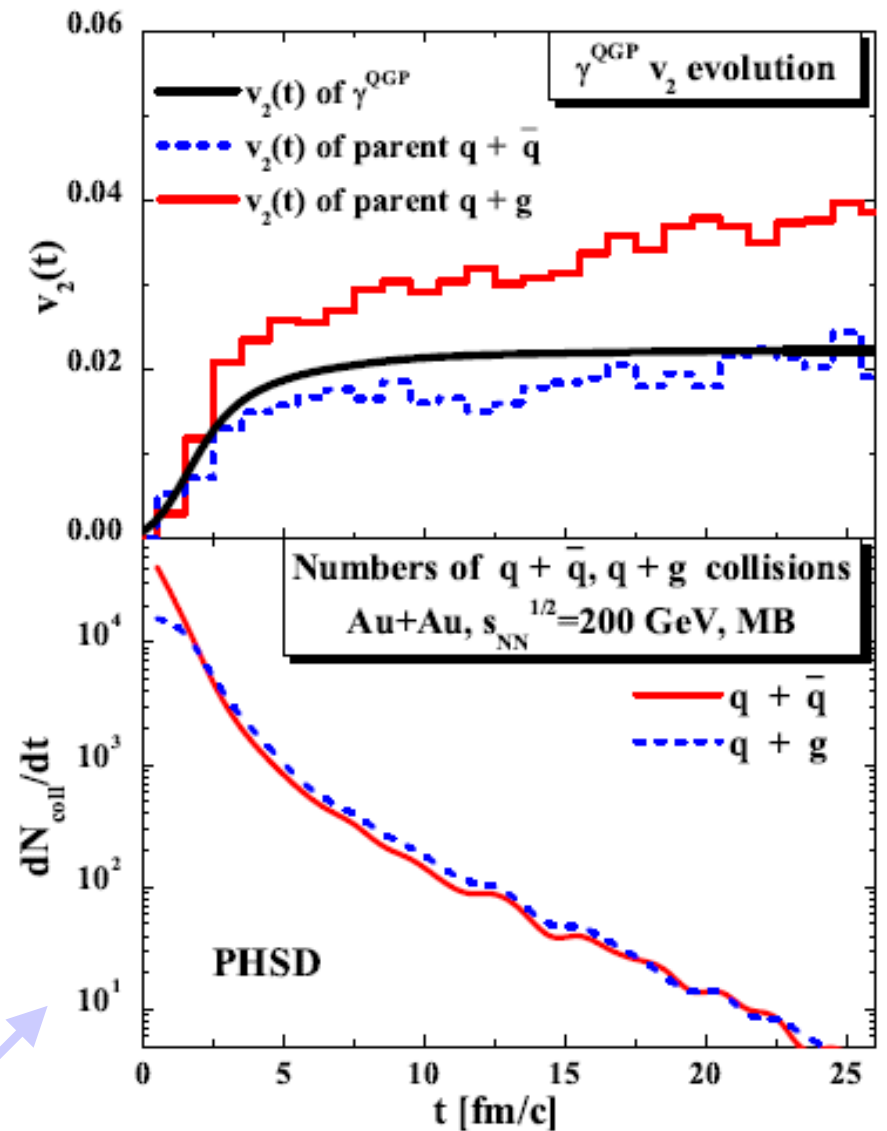
using the soft-photon approximation



# Photon elliptic flow



■ **Strong elliptic flow of photons seen by PHENIX is surprising, if the origin should be the QGP!**

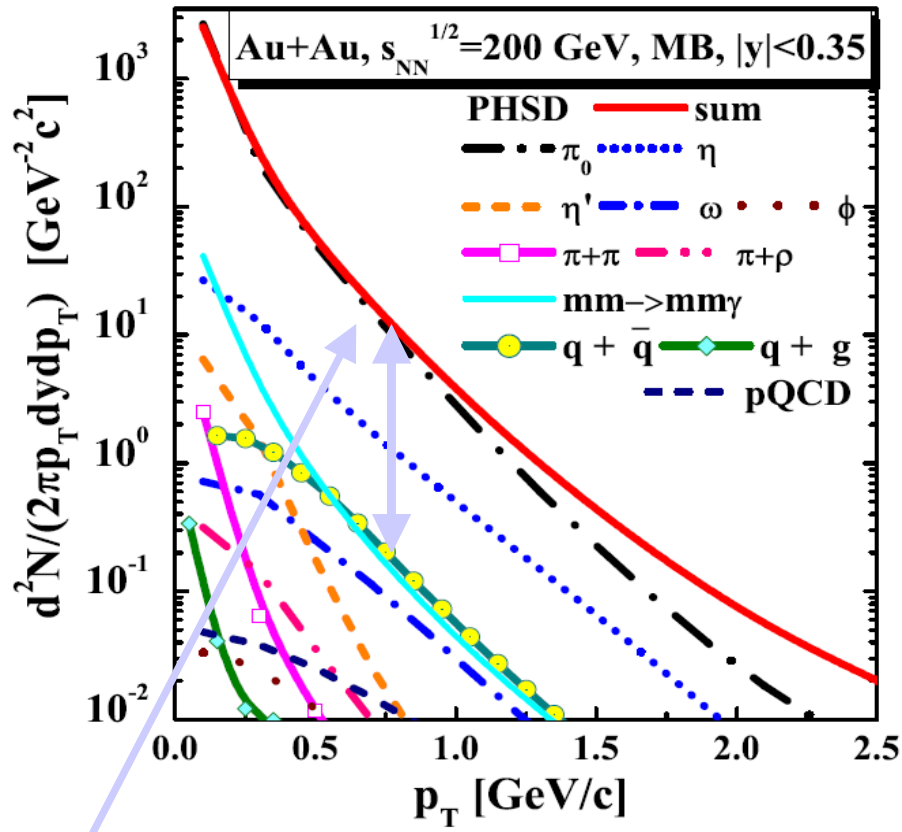


■ **QGP radiation occurs at early times when the flow is not yet developed!**



# Photon spectra at RHIC

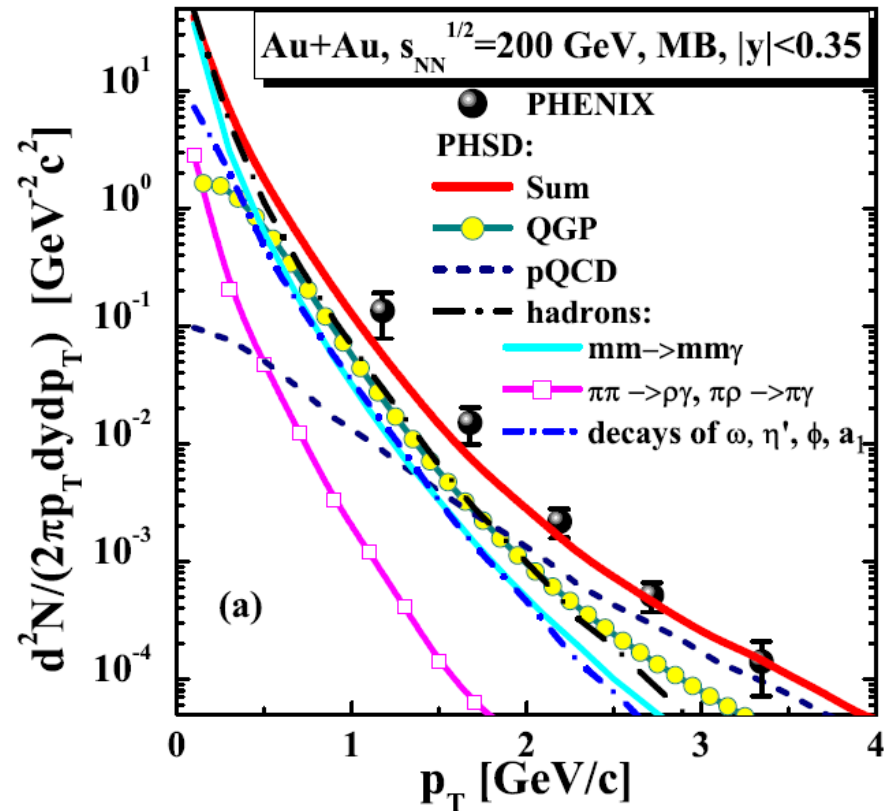
## Inclusive photon spectrum



■  $\pi^0$  and  $\eta$  decays dominate the low  $p_T$  spectra

■ **QGP sources** mandatory to explain the spectrum (~50%), but **hadronic sources** are considerable, too !

## $\pi^0$ and $\eta$ subtracted photon spectrum

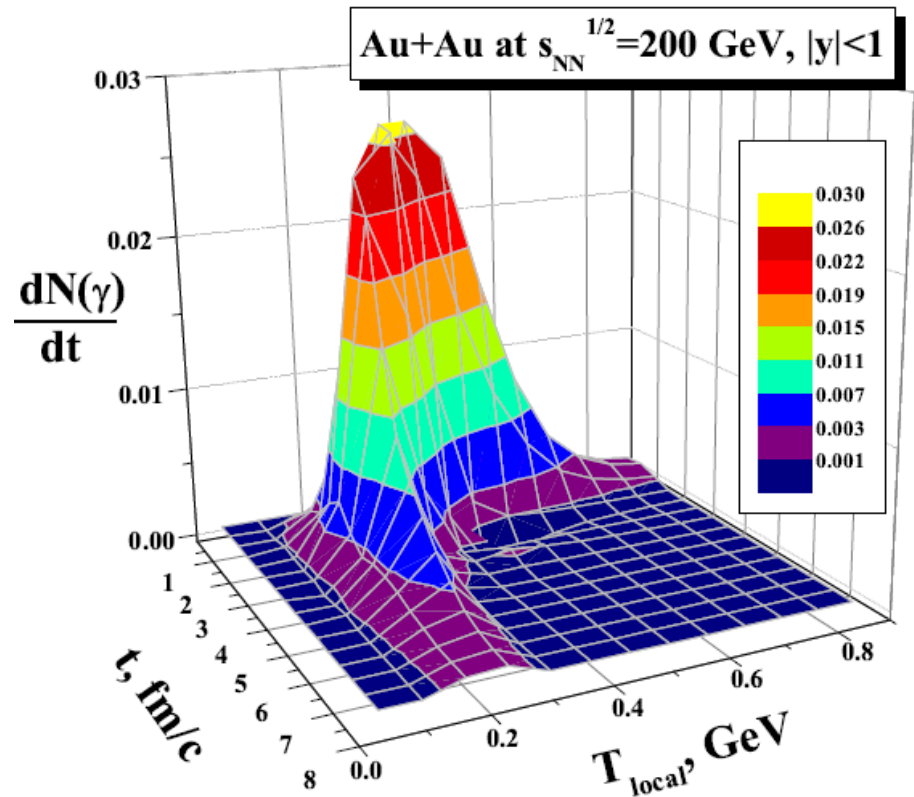
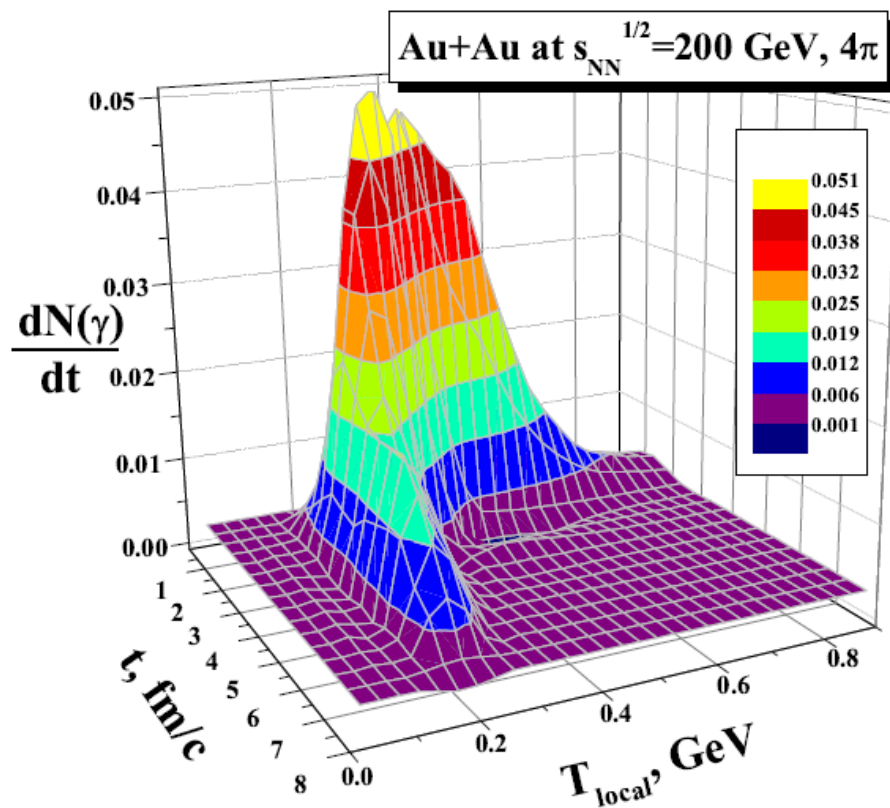


■ The 'effective temperature'  $T_{eff}$ :

The slope parameter $T_{eff}$ (in MeV)			
PHSD			PHENIX
QGP	hadrons	Total	[38]
$260 \pm 20$	$200 \pm 20$	$220 \pm 20$	$233 \pm 14 \pm 19$

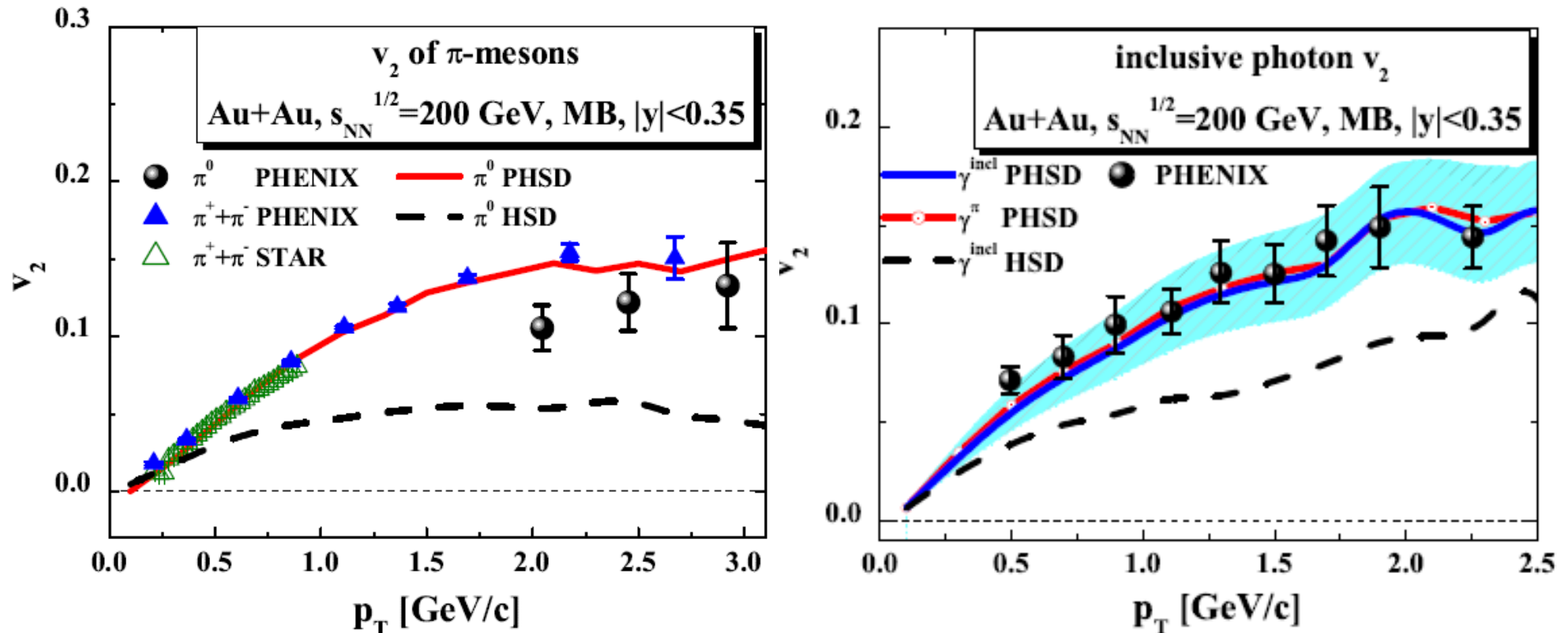
# Time evolution of the photon production rate vs. $T$

- The photon production rate versus time and the local 'temperature' at the production point in  $4\pi$  and **mid-rapidity** Au+Au collisions:



- Broad distribution of 'temperatures'  $\rightarrow$  **no universal 'temperature'** can be assigned to the whole volume of the QGP - even in the mid-rapidity region !

# Inclusive photon elliptic flow



- **Pion elliptic flow** is reproduced in PHSD and underestimated in HSD (i.e. without partonic interactions)
- **→ large inclusive photon  $v_2$**  - comparable to that of hadrons - is reproduced in PHSD, too, because the inclusive photons are dominated by the photons from pion decay

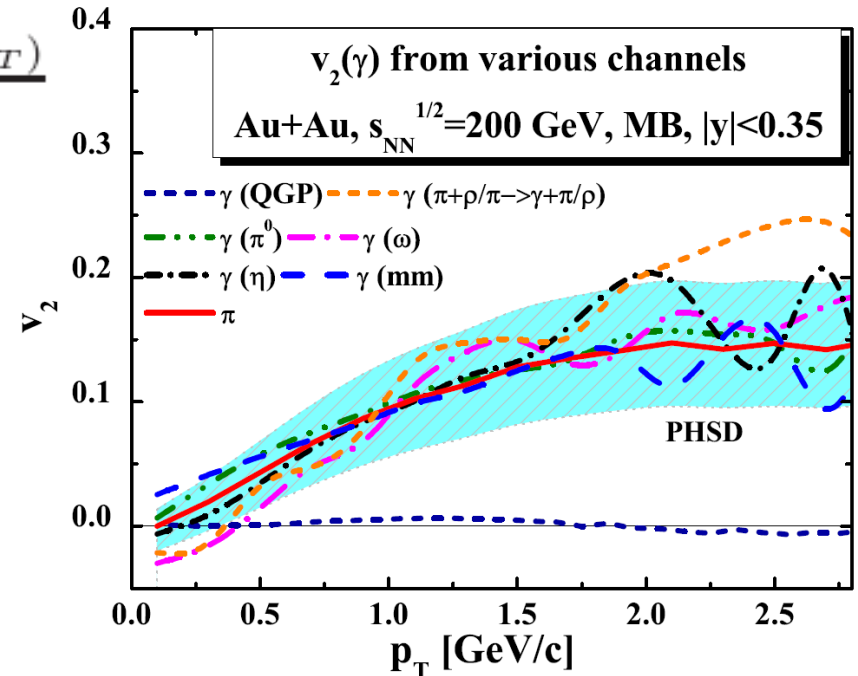
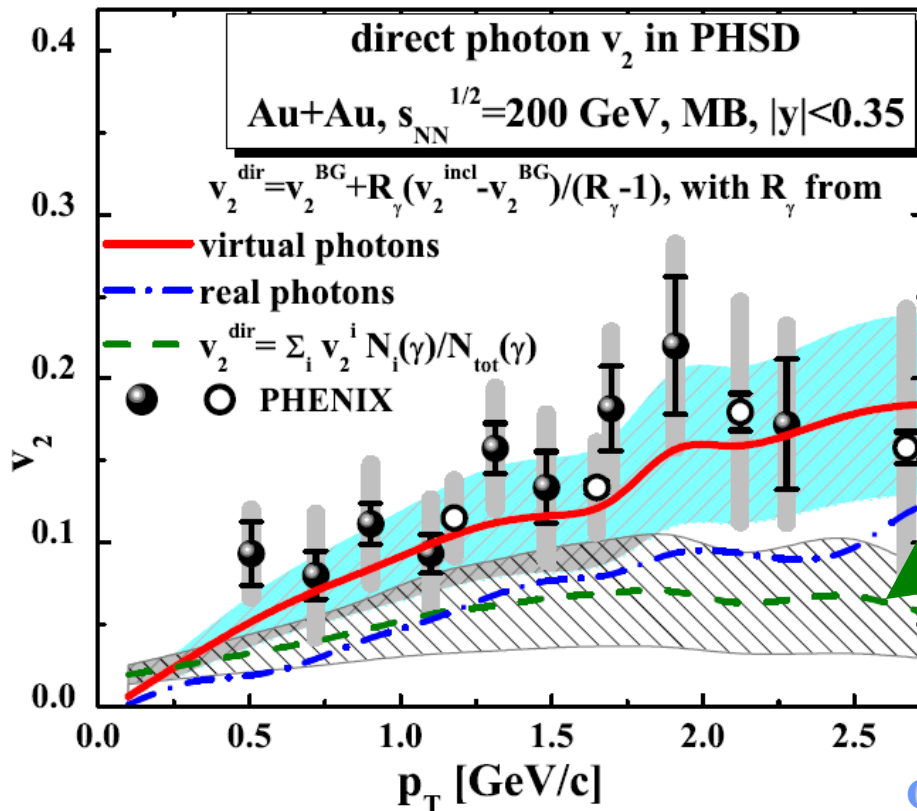
# Elliptic flow from direct photons: method I

▪ **‘Weighted’ method (theor. way):**

direct photon  $v_2$  (in PHSD) = sum of  $v_2$  of the individual channels, using their contributions to the spectrum as the relative  $p_T$ -dependent **weights  $w_i(p_T)$** :

$$v_2(\gamma^{dir}) = \sum_i v_2(\gamma^i) w_i(p_T) = \frac{\sum_i v_2(\gamma^i) N_i(p_T)}{\sum_i N_i(p_T)}$$

$$i = (\underbrace{q\bar{q} \rightarrow g\gamma, qg \rightarrow q\gamma}_{\text{QGP}}, \pi\pi/\rho \rightarrow \rho/\pi\gamma, mm \rightarrow mm\gamma, \text{pQCD})$$



▪  $v_2$  of direct photons in PHSD - as evaluated by the **weighted average** of direct photon channels – **underestimates clearly the exp. data !**



# Elliptic flow from direct photons: method II

- ‚Background‘ subtraction method (exp. way):

$$v_2(\gamma^{dir}) = \frac{R_\gamma v_2(\gamma^{incl}) - v_2(\gamma^{BG})}{R_\gamma - 1} = v_2(\gamma^{BG}) + \frac{R_\gamma}{R_\gamma - 1} (v_2(\gamma^{incl}) - \underline{v_2(\gamma^{BG})})$$

$$R_\gamma = N^{incl} / N^{BG}$$

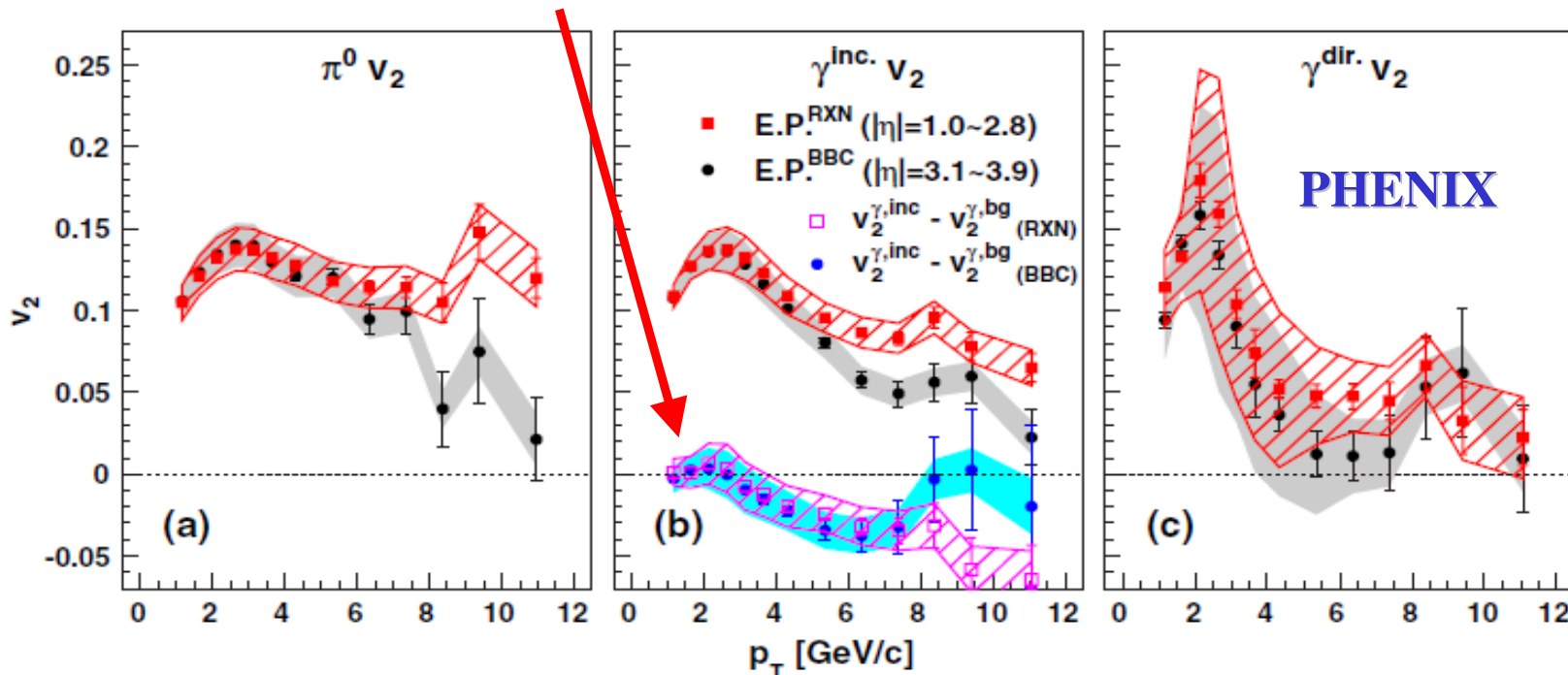
$N^{incl}$  - number of inclusive photons

$N^{BG}$  – number of photons attributed to hadron decays

➔ Problem:  $v_2(\gamma^{BG})$  and  $R_\gamma - ?$

- 1)  $v_2(\gamma^{BG})$  from  $v_2(\pi^0)$  using  $KE_T = m_T - m$  scaling assumption ➔

$$(v_2(\gamma^{incl}) - v_2(\gamma^{BG})) = 0.01$$





▪ **‘Background’ subtraction method (exp. way):**

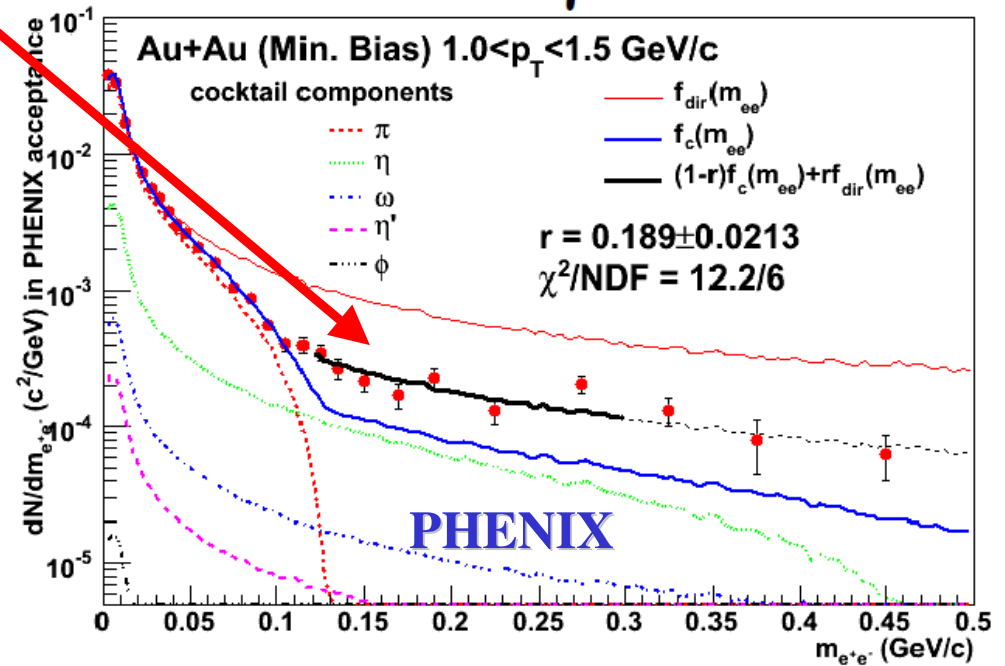
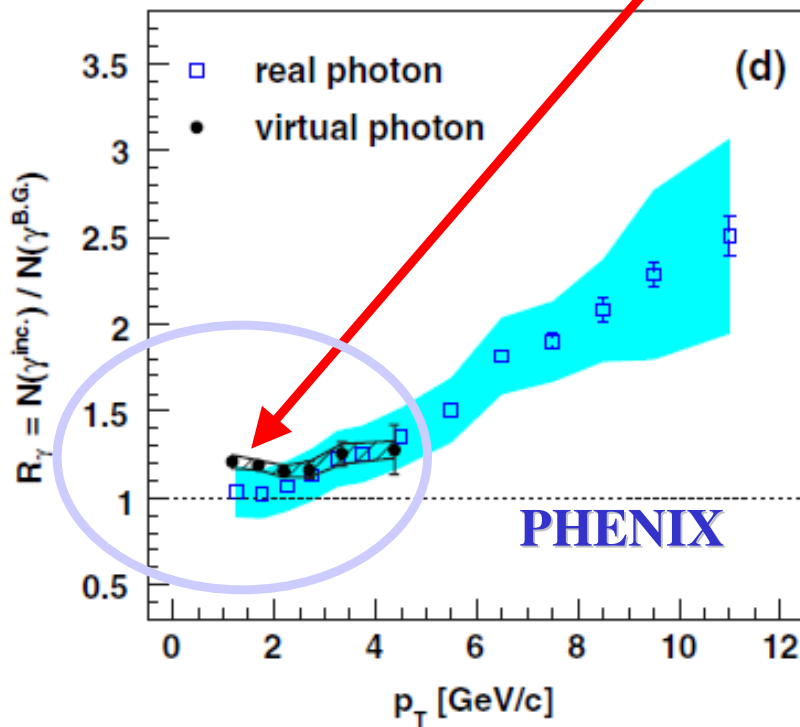
$$v_2(\gamma^{dir}) = \frac{R_\gamma v_2(\gamma^{incl}) - v_2(\gamma^{BG})}{R_\gamma - 1} = v_2(\gamma^{BG}) + \frac{R_\gamma}{R_\gamma - 1} (v_2(\gamma^{incl}) - v_2(\gamma^{BG}))$$

$$R_\gamma = N^{incl} / N^{BG}$$

$N^{incl}$  - number of inclusive photons

$N^{BG}$  – number of photons attributed to hadron decays

▪ **2)  $R_\gamma(p_T)$  for  $p_T < 4$  GeV/c from dilepton spectra at  $M=0.15-0.3$  GeV →**



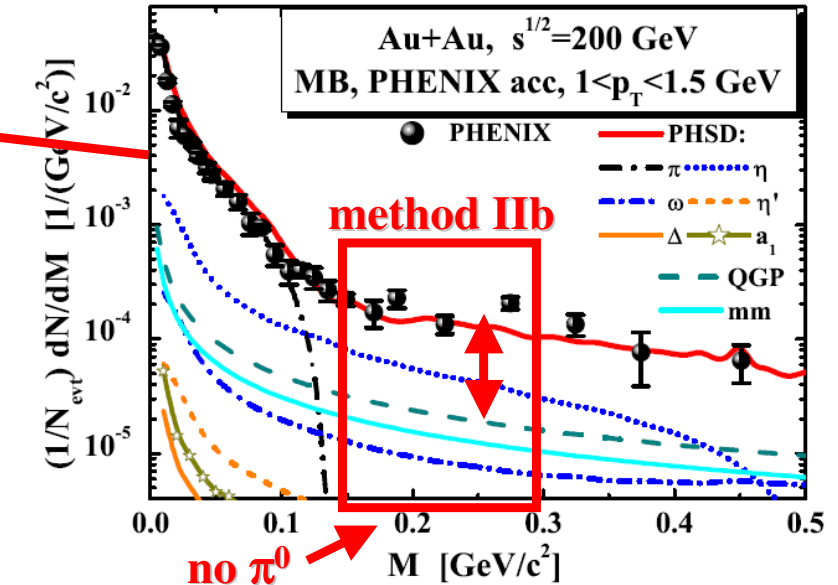
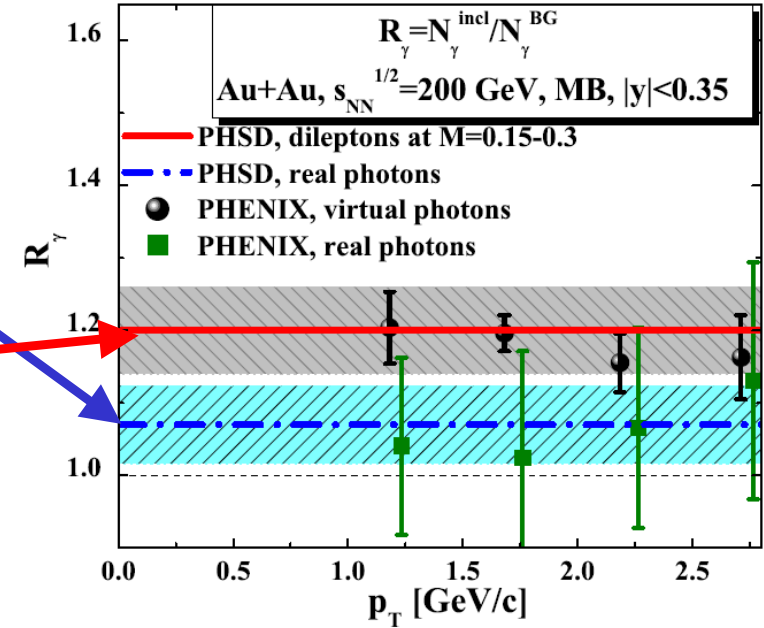
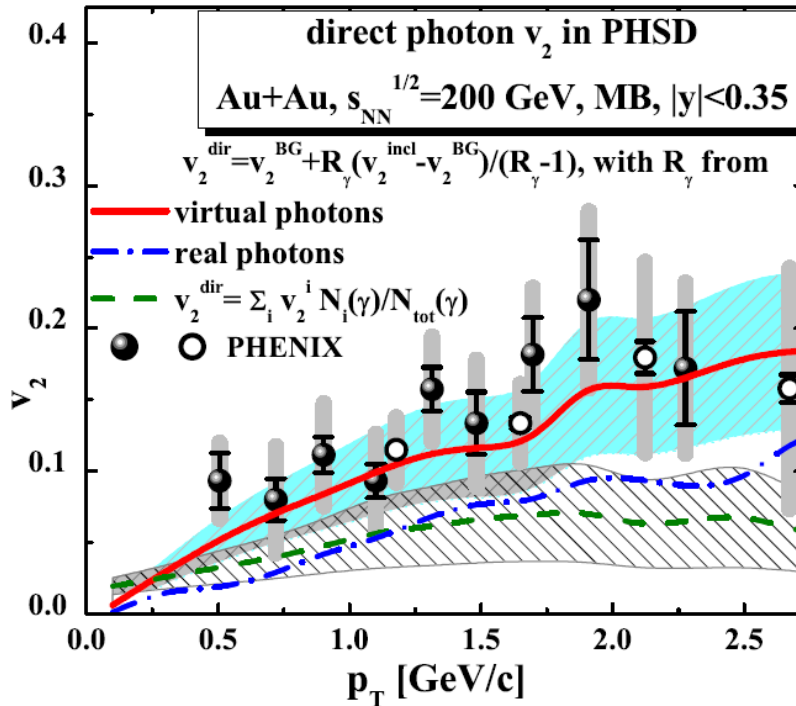
▪ **‘Background’ subtraction method (exp. way):**

$$v_2(\gamma^{dir}) = \frac{R_\gamma v_2(\gamma^{incl}) - v_2(\gamma^{BG})}{R_\gamma - 1}$$

$$R_\gamma = N^{incl} / N^{BG}$$

**IIa) from real photons  $R_\gamma \sim 1.05$**

**IIb) from virtual photons  $R_\gamma \sim 1.2$**



▪  $v_2$  of direct photons in PHSD - as evaluated by the **‘background’ subtraction method IIb** - **is consistent with PHENIX data!**



# Summary

in-equilibrium  
out-of-equilibrium

- **PHSD** provides a consistent description of **off-shell parton dynamics** in line with the lattice QCD equation of state

- minimum of  $\eta/s$  close to  $T_c$   
→ QGP in PHSD behaves almost as a **strongly-interacting liquid**

- minimum of  $\sigma_0/T$  close to  $T_C$   
→ the QCD matter is a **good electric conductor**

- **PHSD** for **HIC**:

- **Direct photons**: the photons produced in the QGP contribute about **50%** to the observed spectrum but have **small  $v_2$**

- **The large measured ‘direct photon  $v_2$ ’** – comparable to that of hadrons – is attributed to **intermediate hadronic scattering channels and hadronic resonance decays** not subtracted from the data;  
**the value of  $v_2$  is sensitive to the hadronic ‘background’ subtraction method!**

- The **QGP phase** causes the strong elliptic flow of photons **indirectly** by enhancing the  $v_2$  of final hadrons due to the partonic interactions in terms of explicit parton collisions and the mean-field potentials!



# PHSD group

**Wolfgang Cassing (Giessen Univ.)**

**Volodya Konchakovski (Giessen Univ.)**

**Olena Linnyk (Giessen Univ.)**

**Thorsten Steinert (Giessen Univ.)**

**Elena Bratkovskaya (FIAS & ITP Frankfurt Univ.)**

**Vitalii Ozvenchuk (now in Nantes Univ.)**

**Rudy Marty (FIAS, Frankfurt Univ.)**

**Hamza Berrehrah (FIAS, Frankfurt Univ.)**

**Daniel Cabrera (ITP&FIAS, Frankfurt Univ.)**

**Taesoo Song (ITP&FIAS, Frankfurt Univ.)**

**Andrej Ilner (HGS-HIRe Frankfurt Univ.)**

## **External Collaborations:**

**SUBATECH, Nantes Univ. :**

**Jörg Aichelin**

**Christoph Hartnack**

**Pol-Bernard Gossiaux**

**Texas A&M Univ.:**

**Che-Ming Ko**

**JINR, Dubna:**

**Vadim Voronyuk**

**Viatcheslav Toneev**

**Kiev Univ.:**

**Mark Gorenstein**

**Barcelona Univ.**

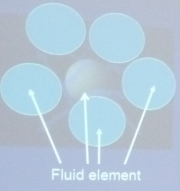
**Laura Tolos, Angel Ramos**







approximated by noise ?



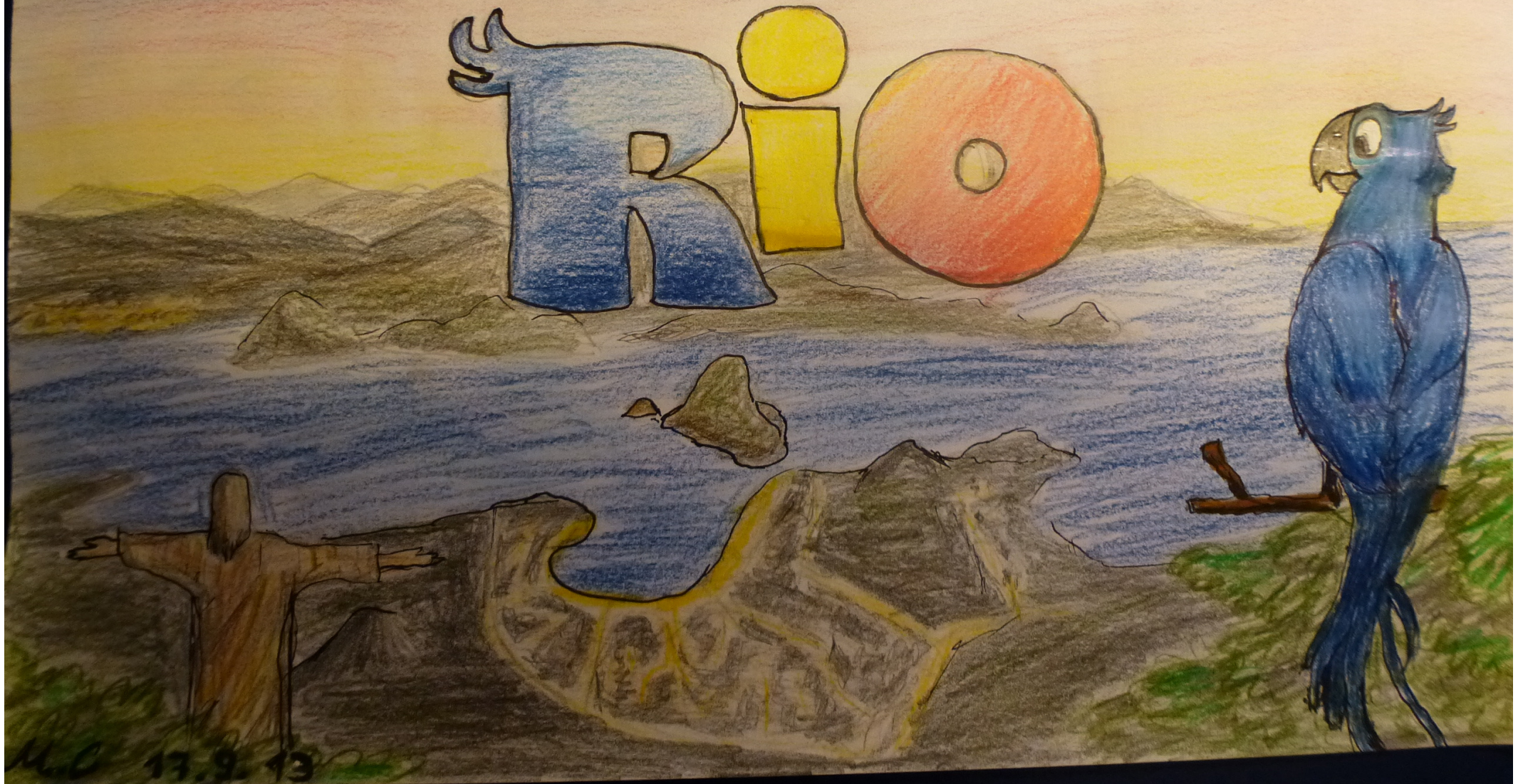
Fluid element

Indeterminacy of fluid elements





**Happy birthday, Takeshi!**



17.9.13